

Waves I

EPS131, Introduction to Physical Oceanography and Climate

Dept of Earth and Planetary Sciences, Harvard University

Eli Tziperman



https://en.wikipedia.org/wiki/File:Tsunami_by_hokusai_19th_century.jpg

Surface ocean waves



look at 2:57–4 minutes

<https://www.youtube.com/watch?v=RMUxSwUB0p0>

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Internal waves and ocean mixing

show 1:40-3:30

first 20 sec, and then jump to 1:11

<https://www.youtube.com/watch?v=x7GXLJQ2Zn0>

<https://swot.jpl.nasa.gov/resources/147/internal-wave-tank-demonstration/>

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Notes

1 Inertial oscillations

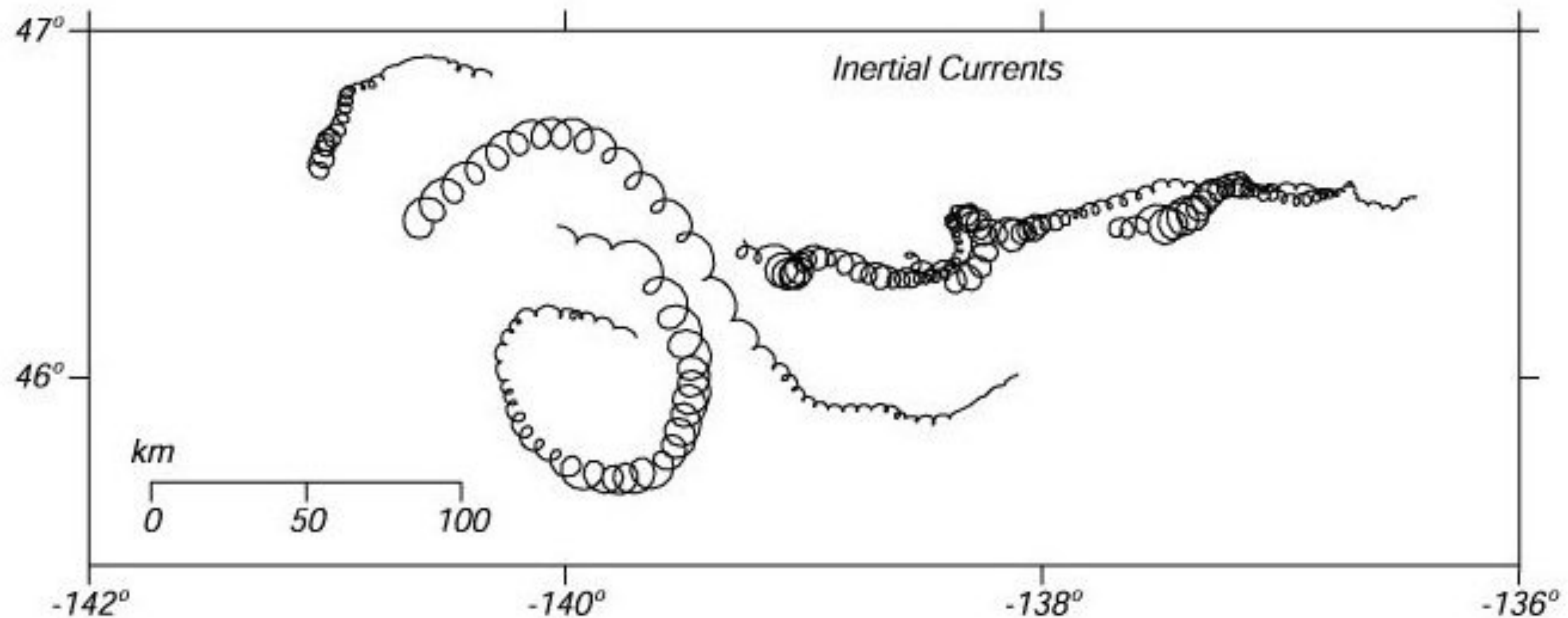
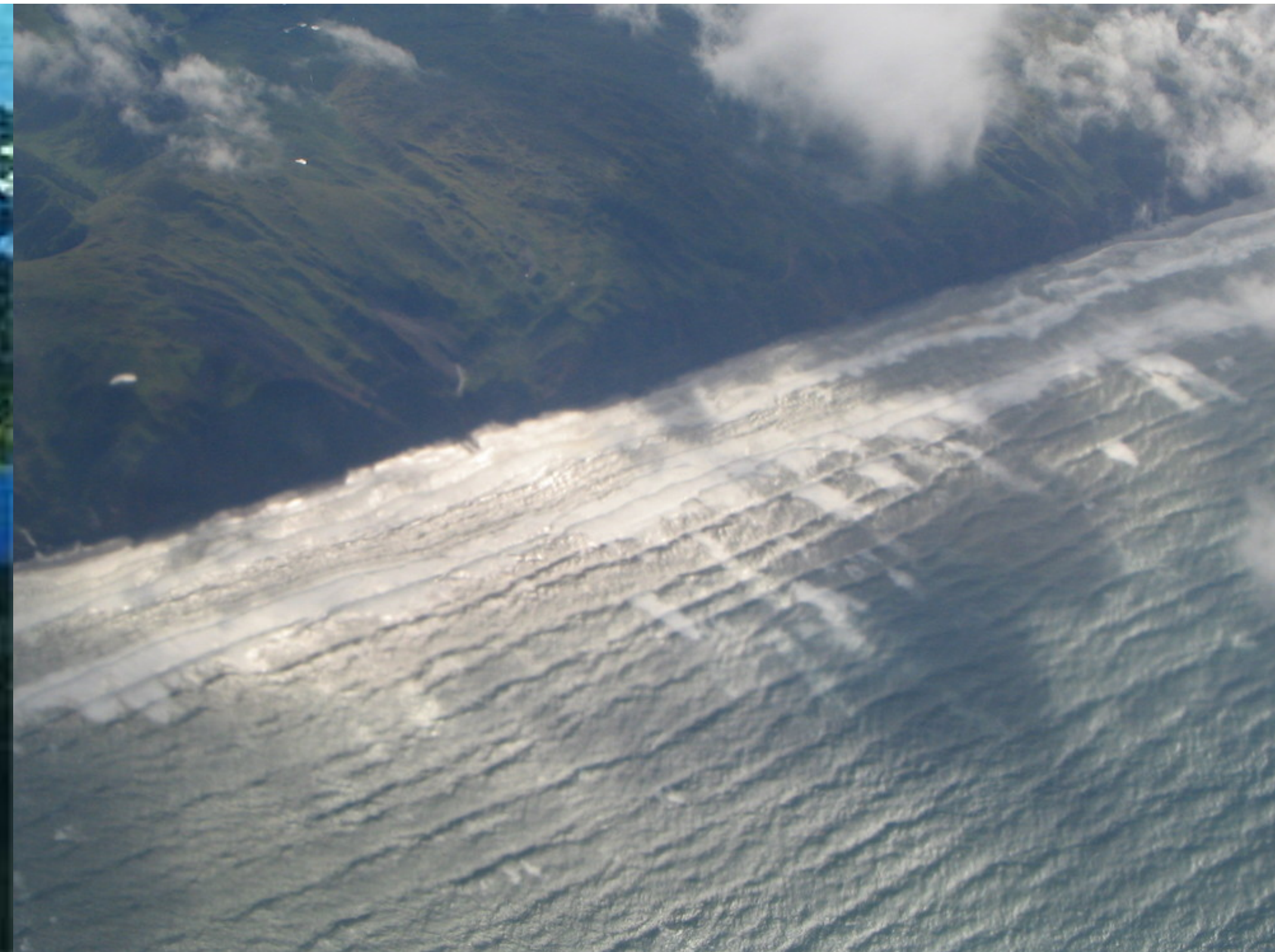


Figure 9.1 Inertial currents in the North Pacific in October 1987 (days 275-300) measured by holey-sock drifting buoys drogued at a depth of 15 meters. Positions were observed 10-12 times per day by the Argos system on NOAA polar-orbiting weather satellites and interpolated to positions every three hours. The largest currents were generated by a storm on day 277. Note: these are not individual eddies. The entire surface is rotating. A drogue placed anywhere in the region would have the same circular motion. From van Meurs (1998).

Miniquiz

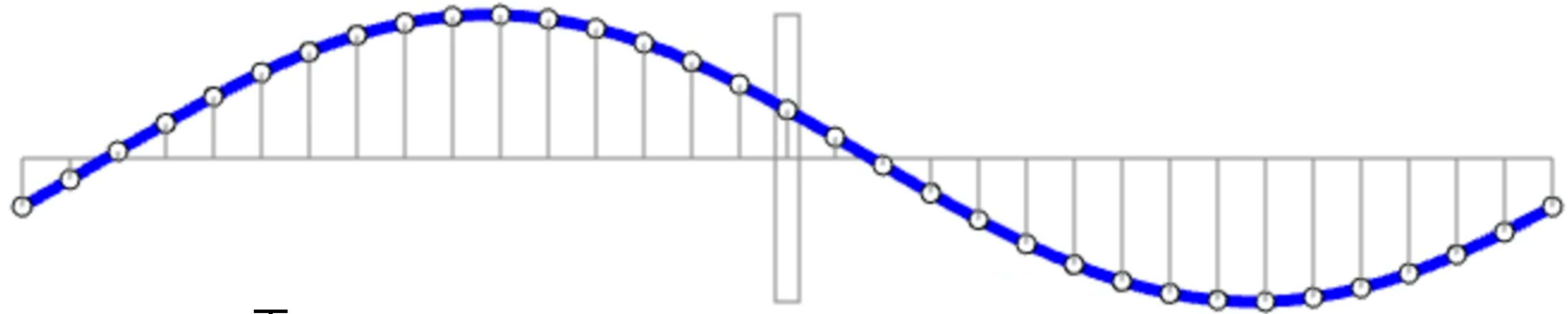
$F=ma$ for inertial oscillations

Notes

2 Wave basics: Definitions/ Phase velocity/ Group velocity

Why do waves arrive parallel to the coastline?

2 Wave basics: Definitions/ Phase velocity/ Group velocity



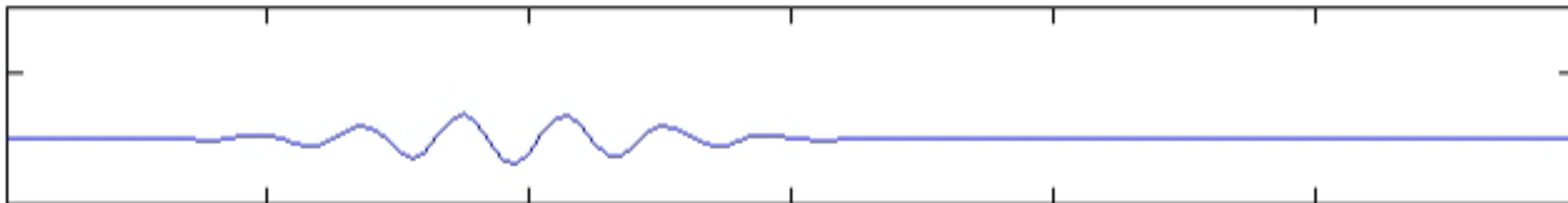
Transverse waves surendranath.org/GPA/Waves/TW01/TW01.html



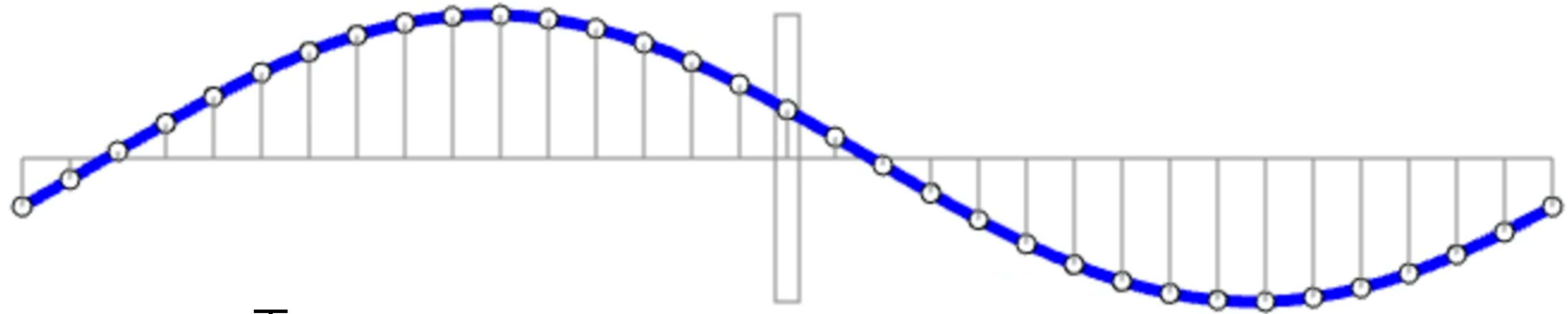
longitudinal waves <https://www.surendranath.org/GPA/Waves/LW01/LW01.html>

surface gravity wave in deep water

Phase speed vs group speed



2 Wave basics: Definitions/ Phase velocity/ Group velocity



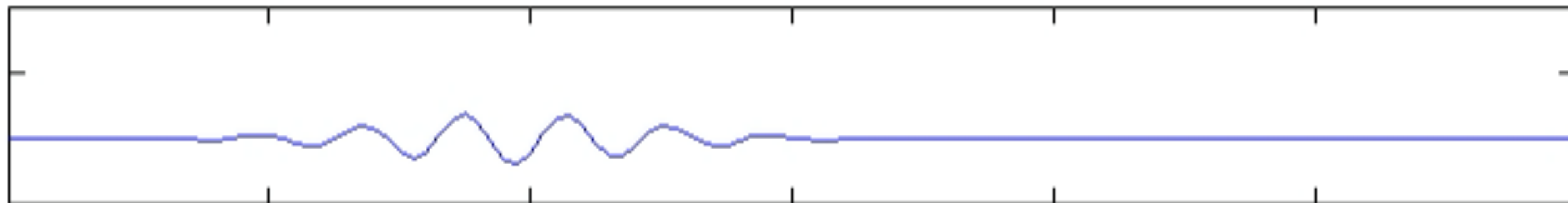
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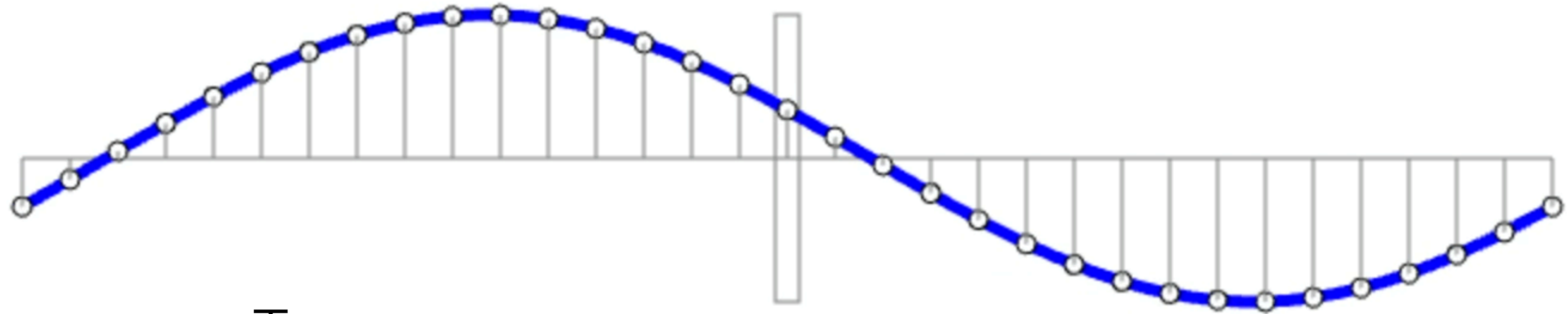
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2 Wave basics: Definitions/ Phase velocity/ Group velocity



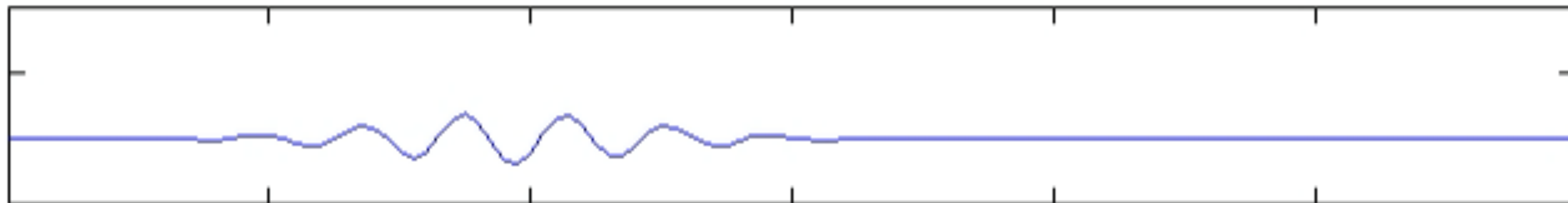
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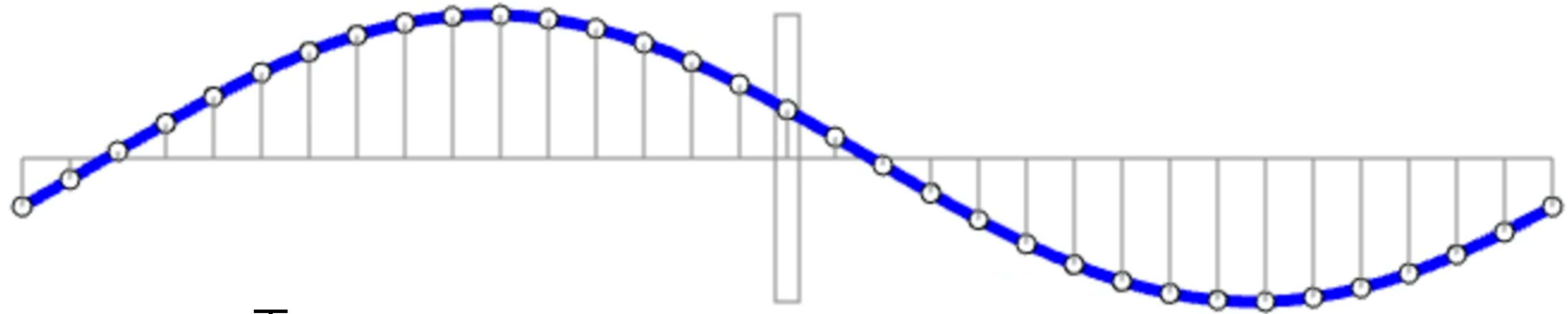
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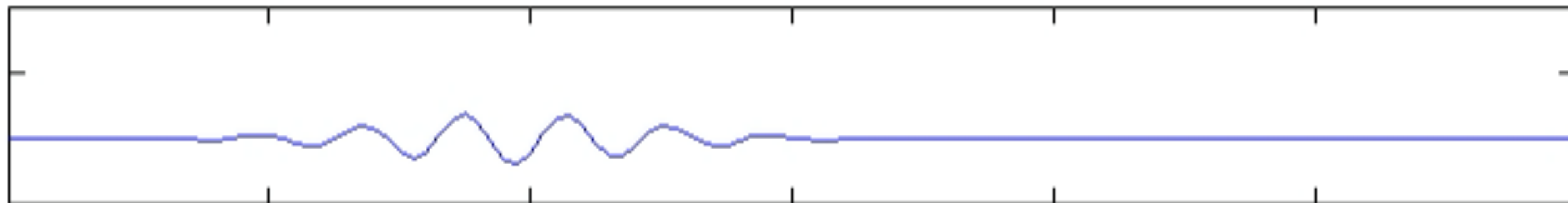
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surface gravity wave in deep water

Phase speed vs group speed



Notes

3 Surface gravity waves – without rotation

3.1 dimensional analysis

miniquiz

dispersion relation from dimensional arguments

Notes

3 Surface gravity waves – without rotation

3.2 Shallow water 1d mass conservation

3.3 Shallow water 1d momentum equation

Miniquiz

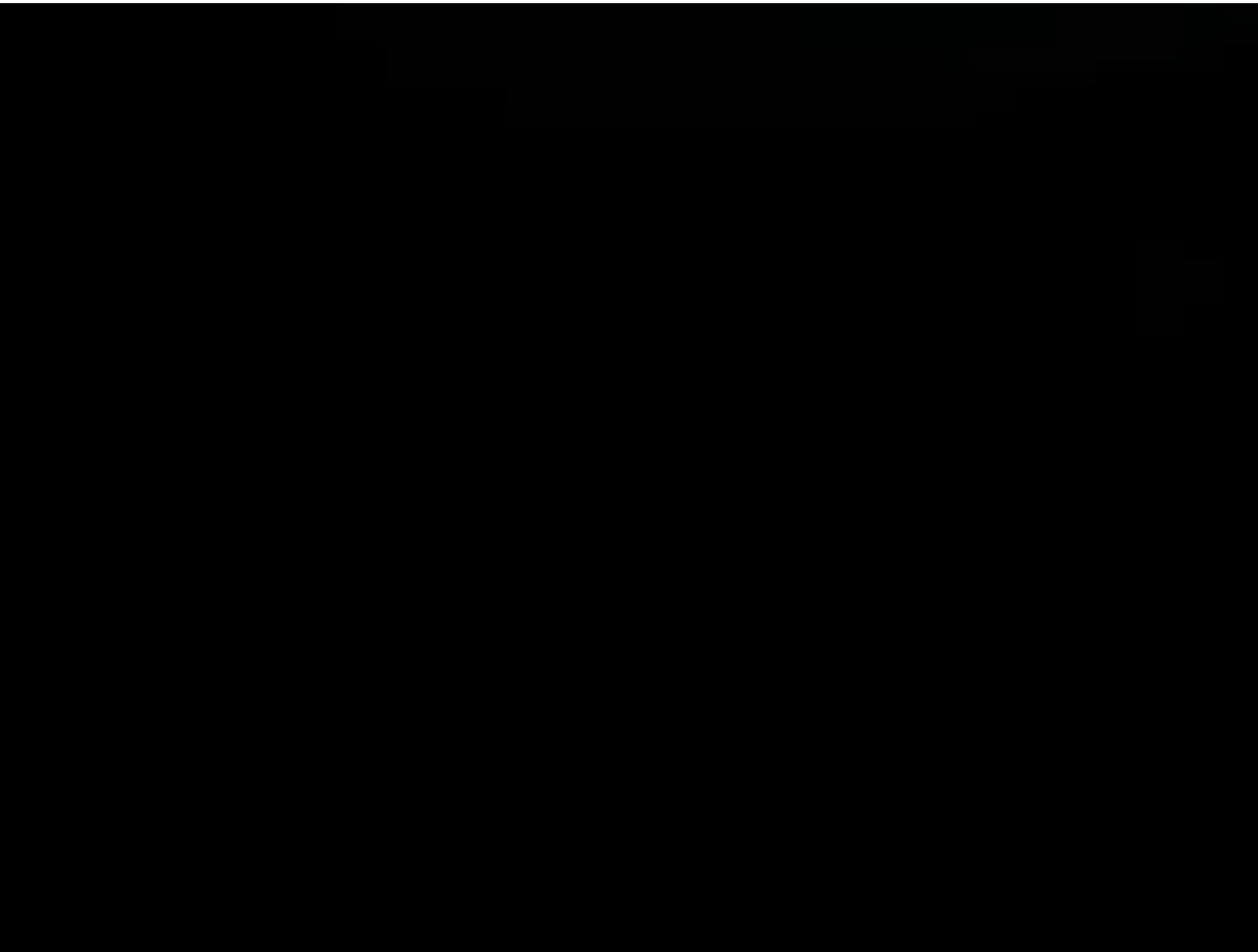
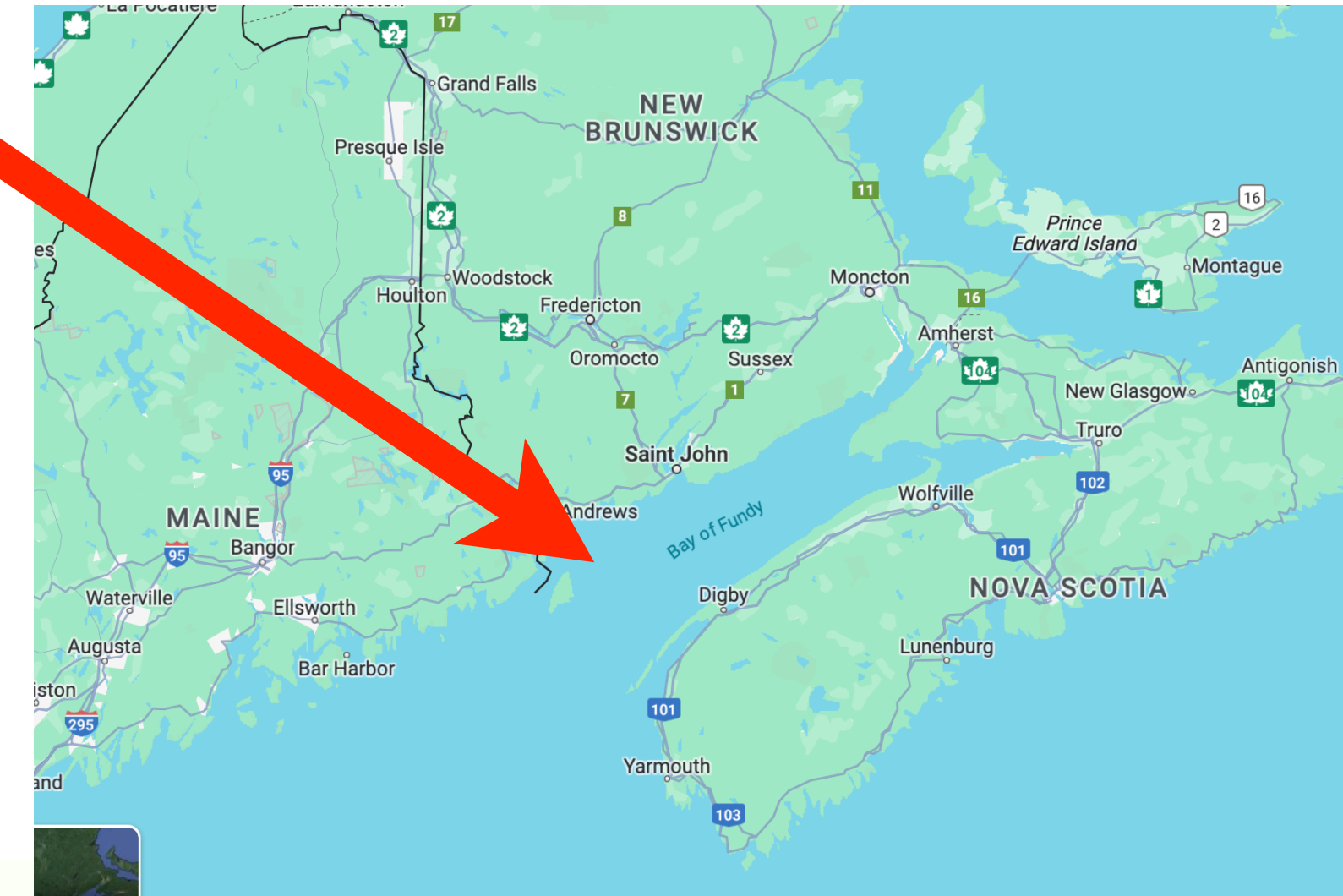
derive the shallow water 1d wave equation, use it to find the dispersion relation

Notes

3 Surface gravity waves – without rotation

3.5 Particle trajectories (for shallow water waves w/o rotation)

Tides in the Bay of Fundy

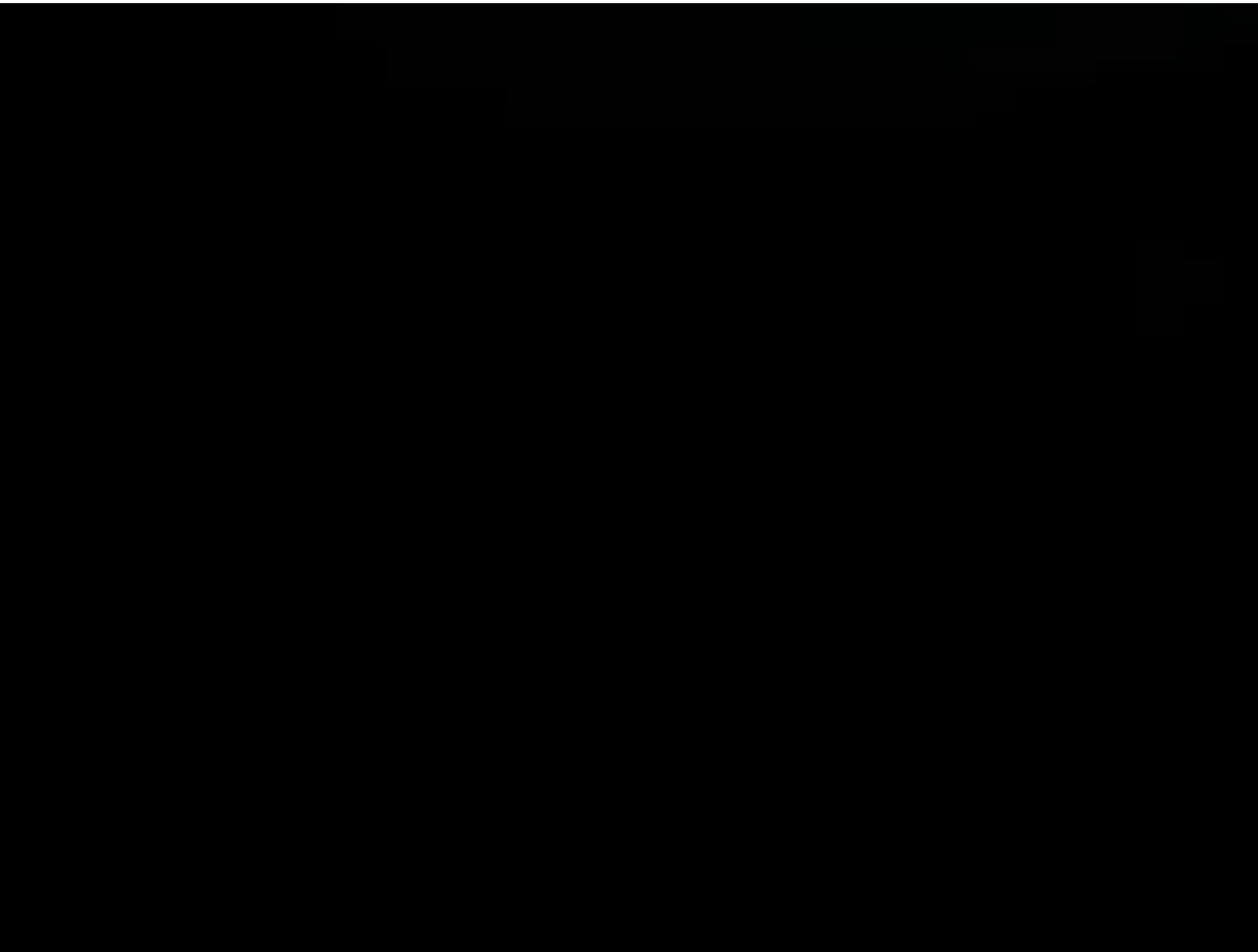
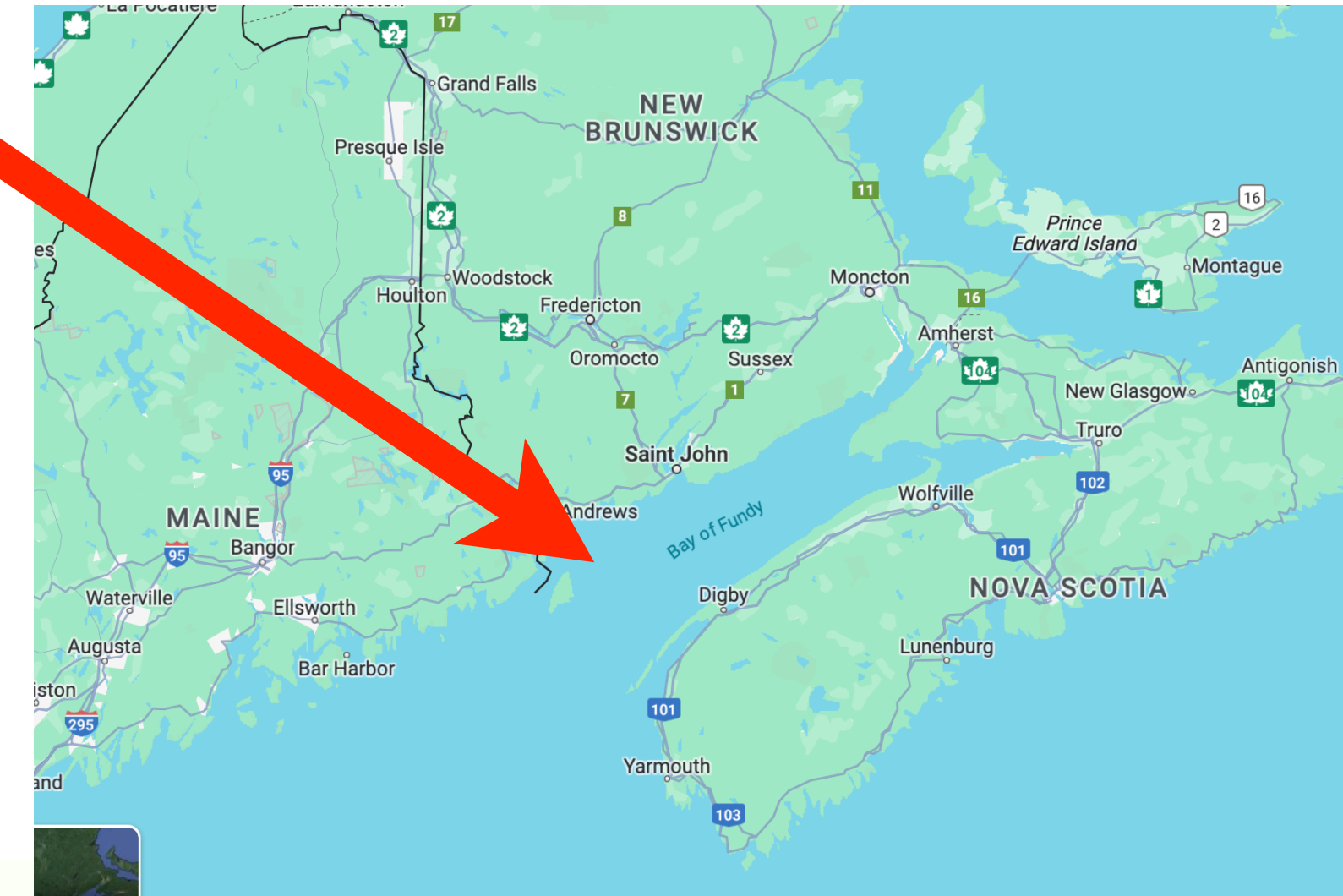


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<https://www.youtube.com/watch?v=u3LtEF9WPt4>

Tides in the Bay of Fundy

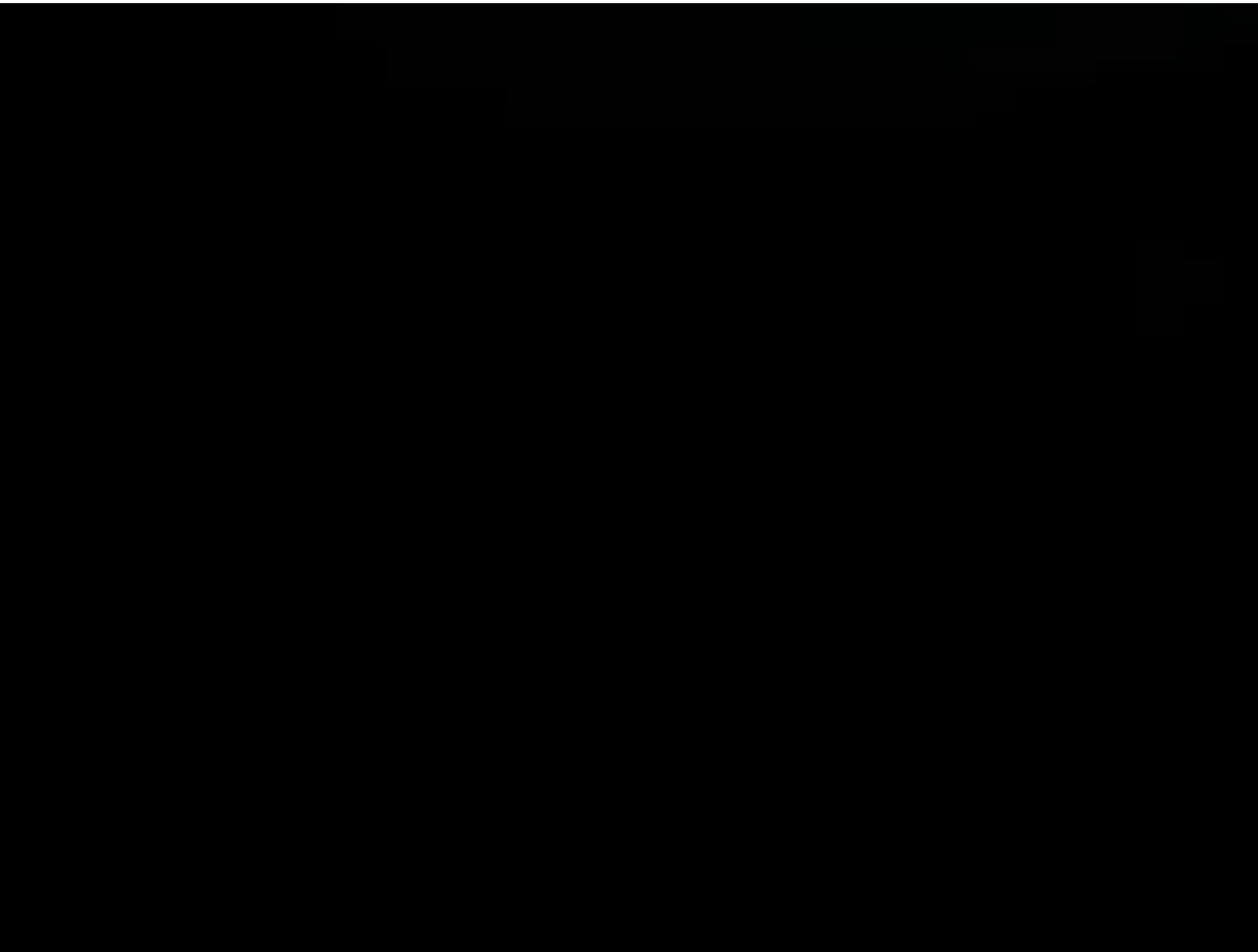
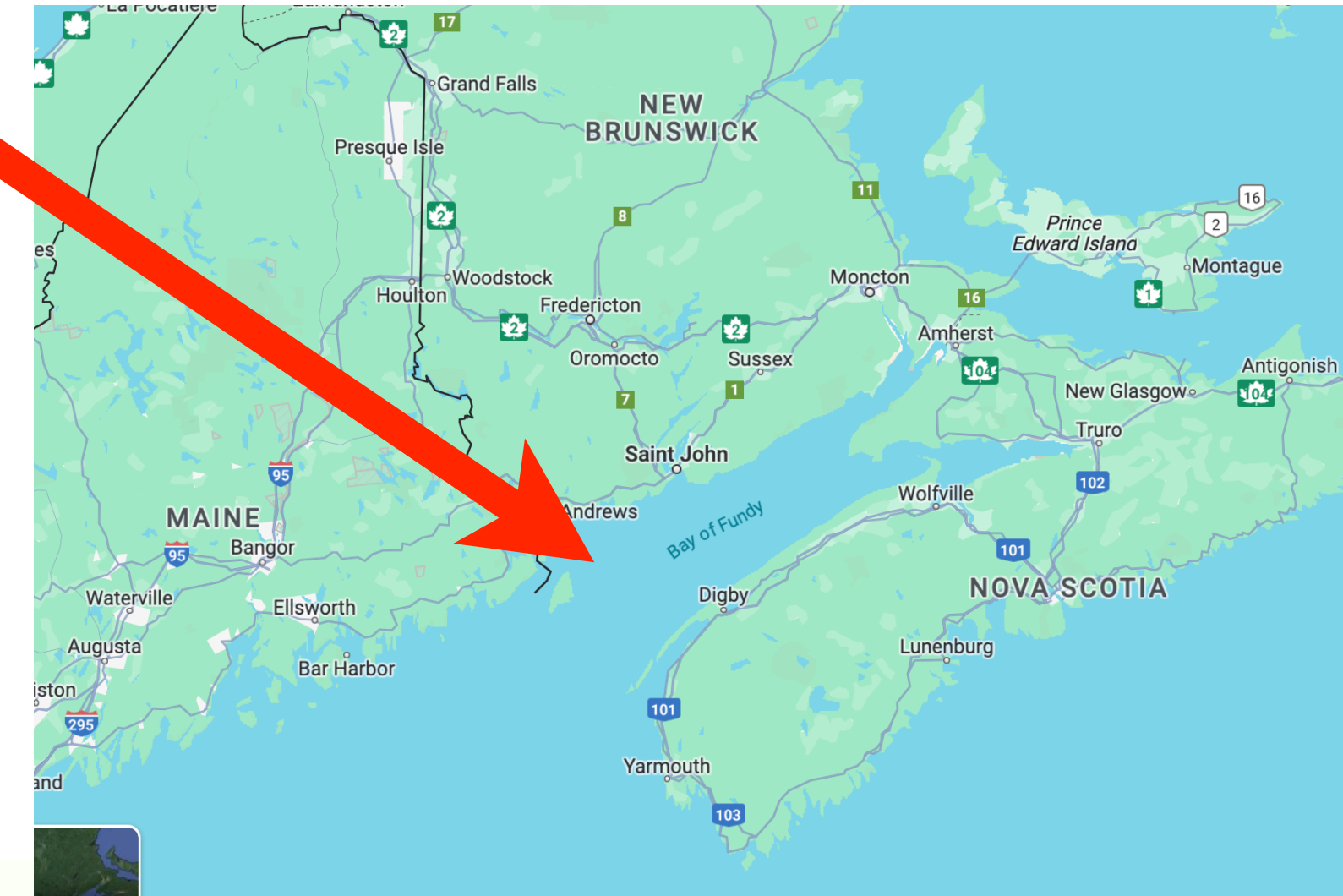


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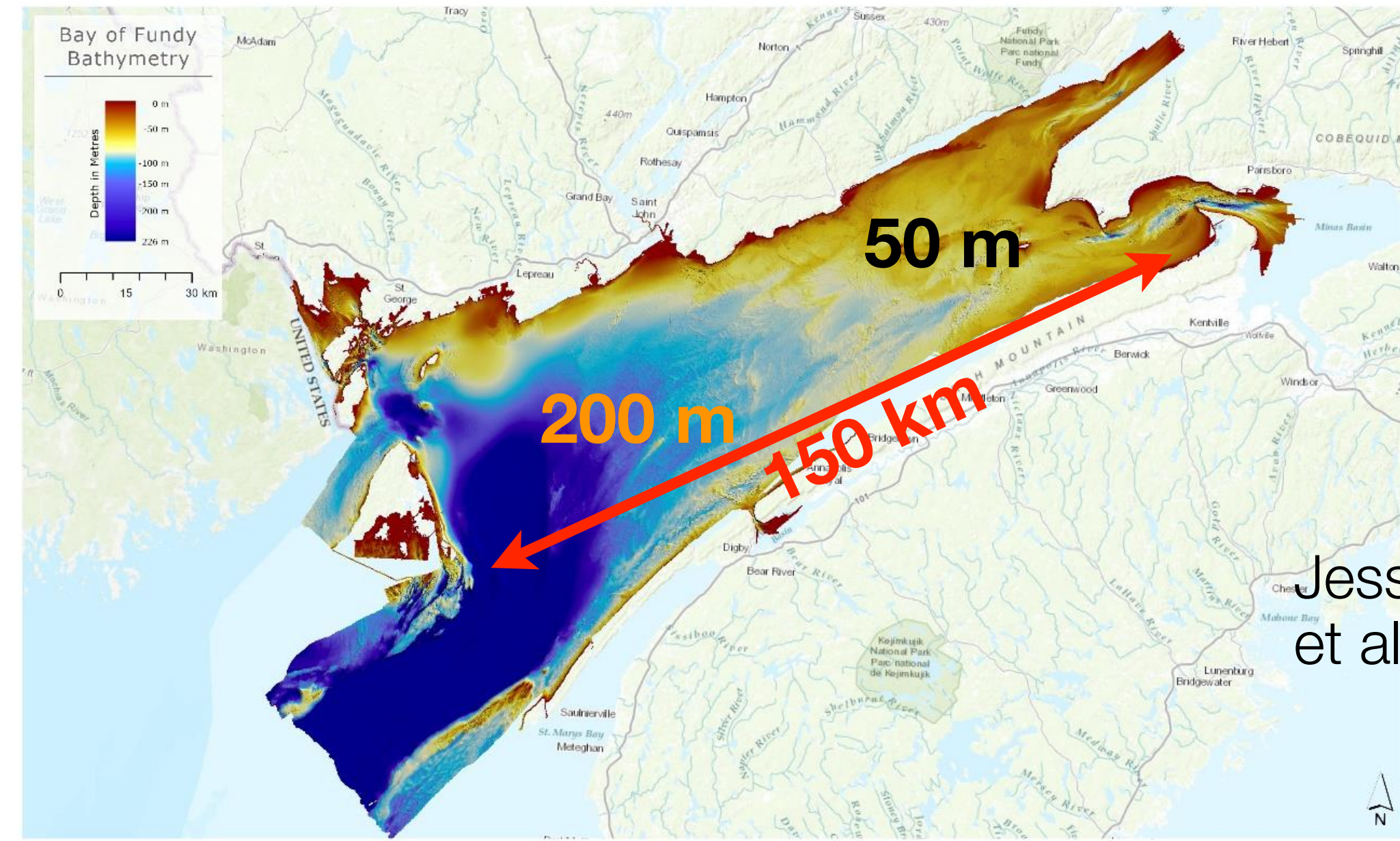
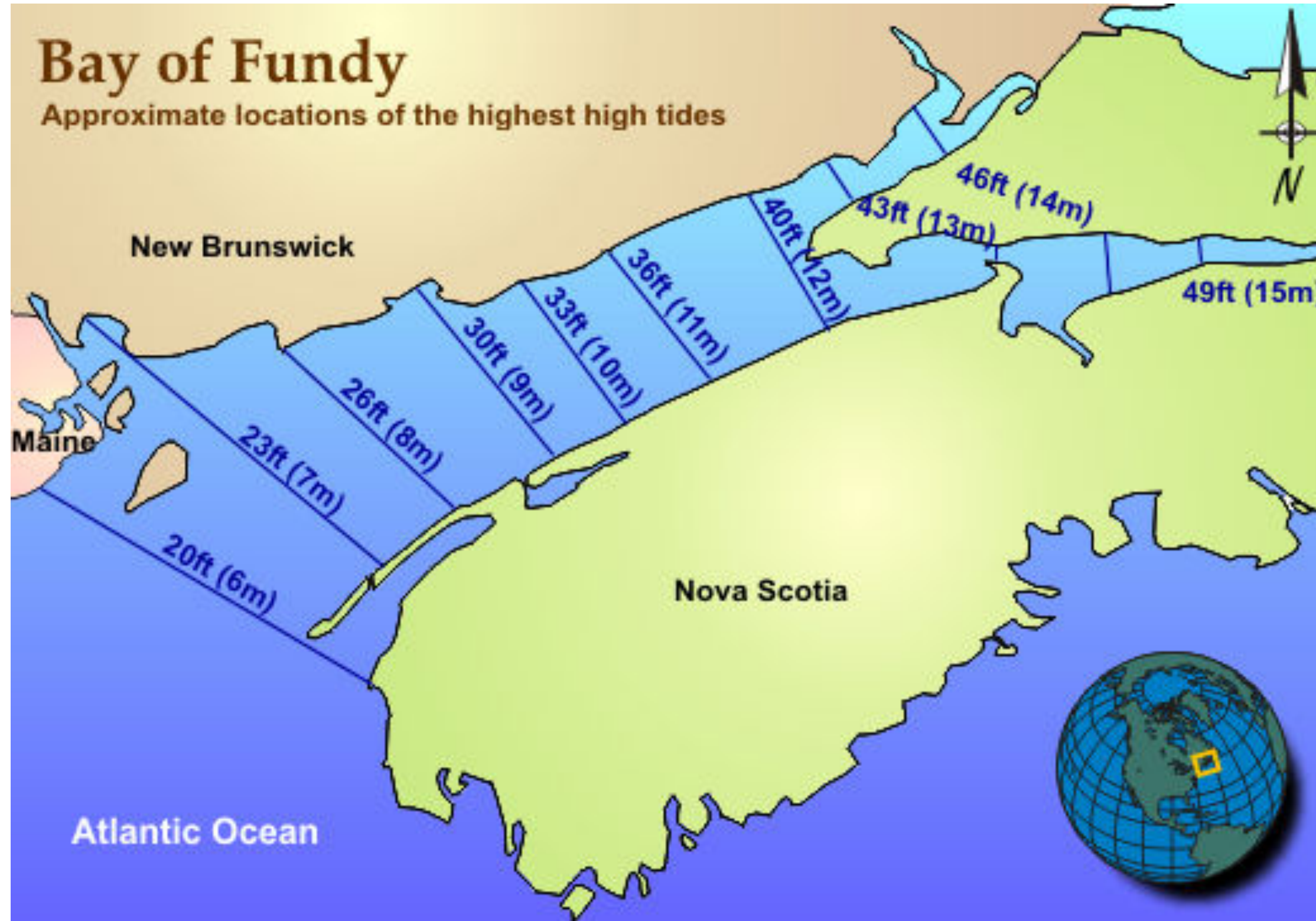
Notes

3 Surface gravity waves – without rotation

3.6 Standing waves (springs demo!)

3.7 Tidal resonance

Bay of Fundy: The Highest Tides in the World



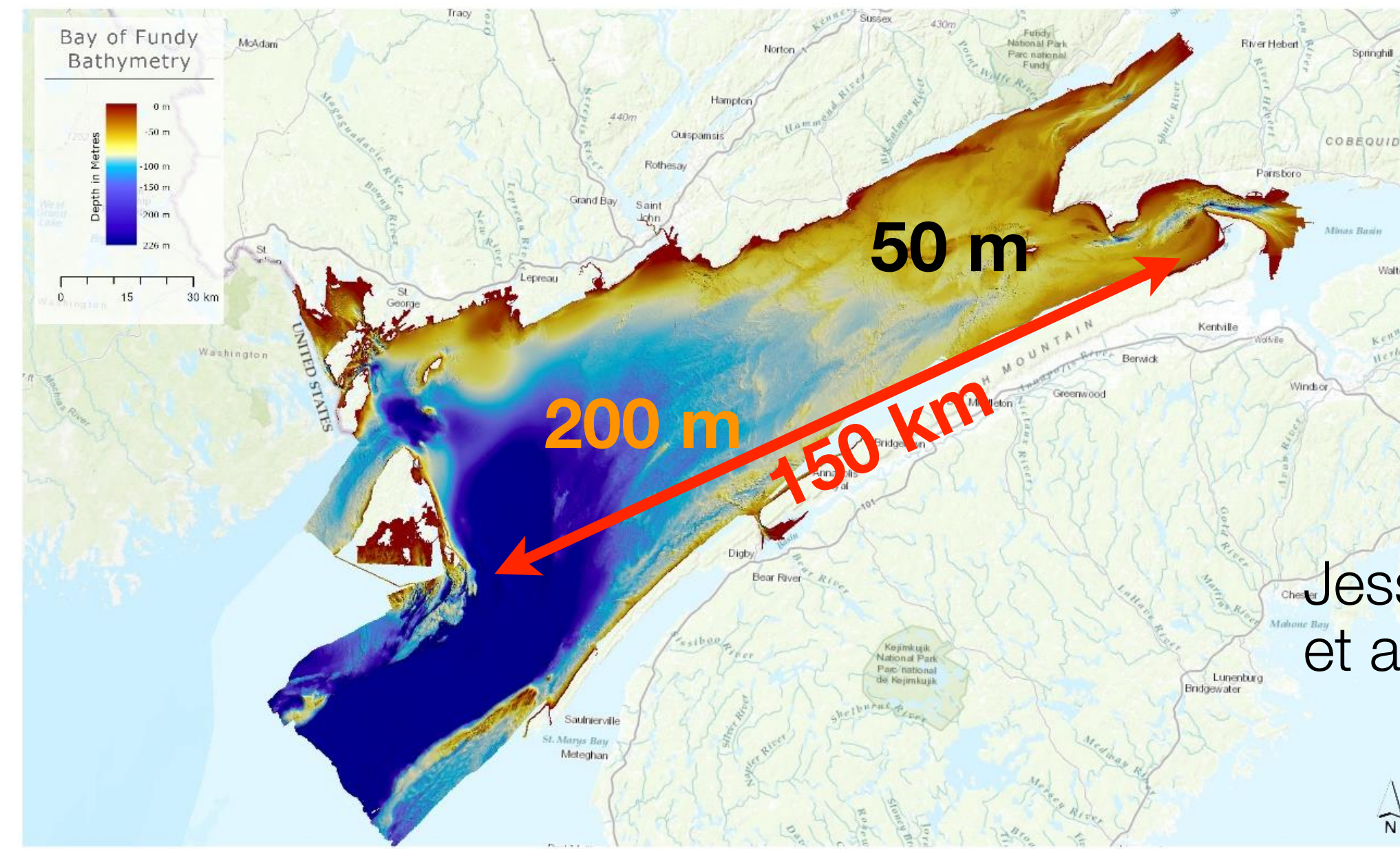
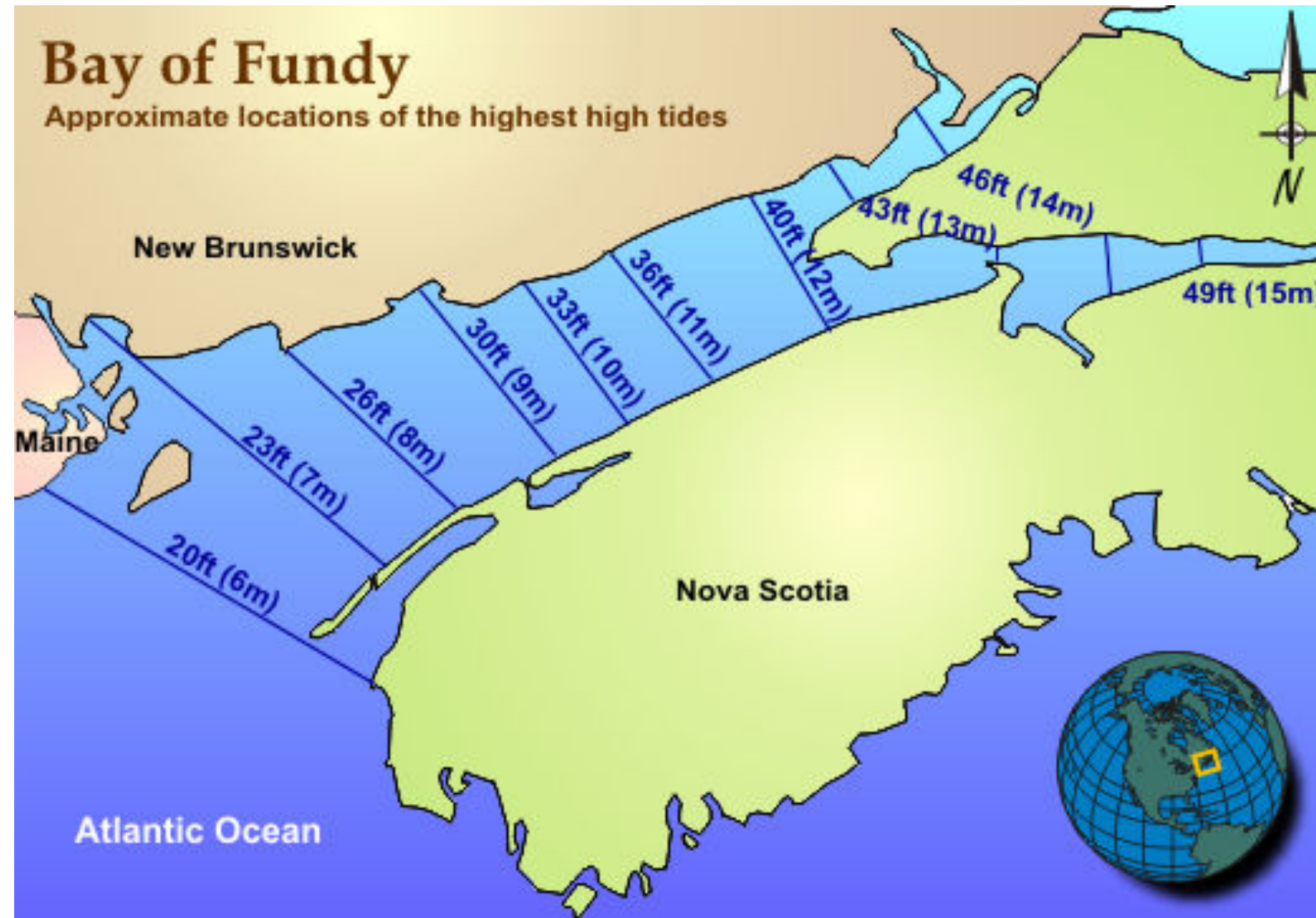
Jessica A. Sameoto et al 2020

<https://www.noaa.gov/ocean/fundy-max>



“While the Earth's average tide-driven variation in sea level is 3 feet, the water level near Wolfville, in Nova Scotia's Minas Basin, can be as much as 53 feet (16 m) higher than at low tide.”

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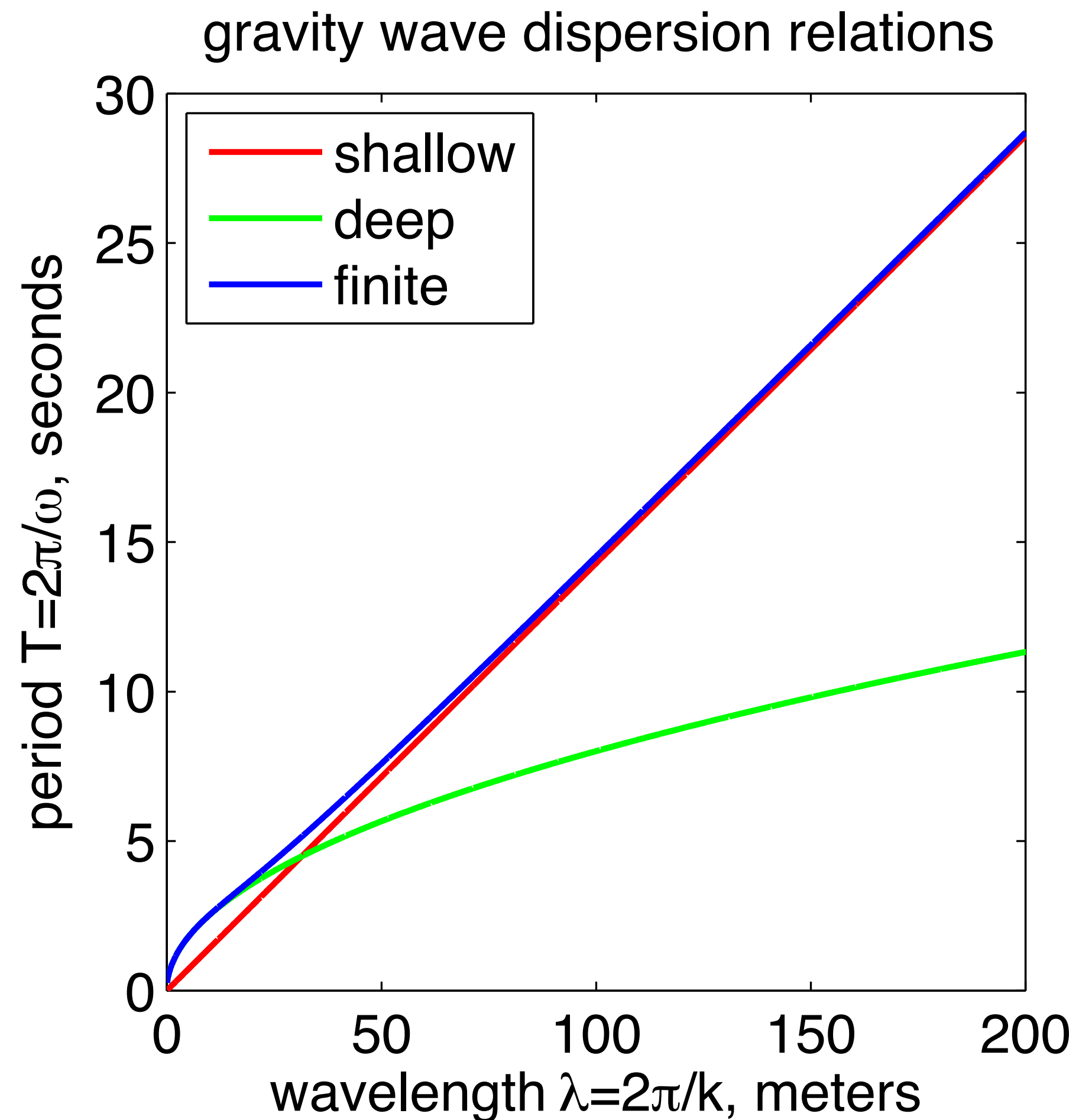


Notes

3 Surface gravity waves – without rotation

3.8 Deep 1d water waves scaling argument, particle trajectories

3.9 Finite ocean depth & limits of shallow & deepwater

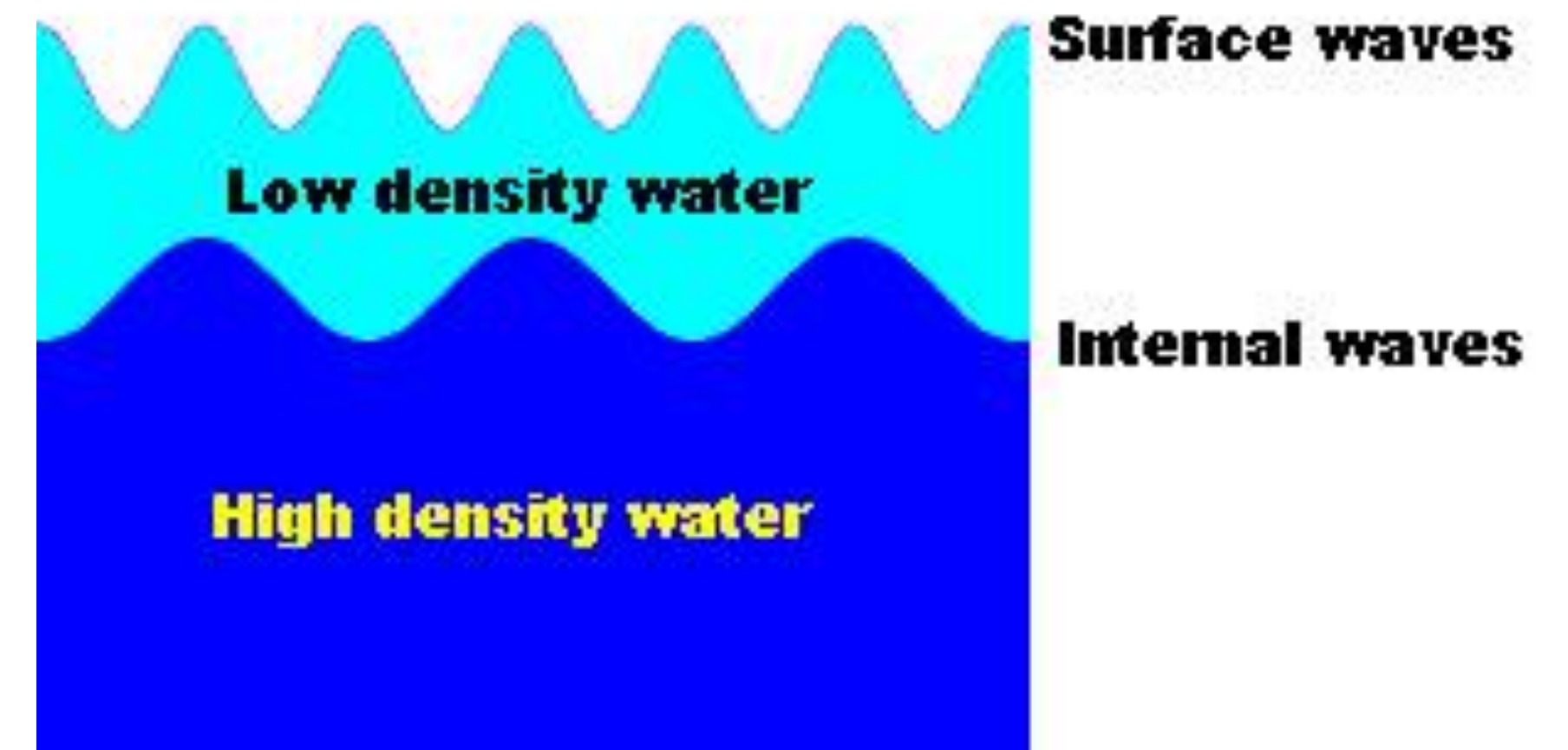


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deep gravity waves dispersion relation from dimensional arguments

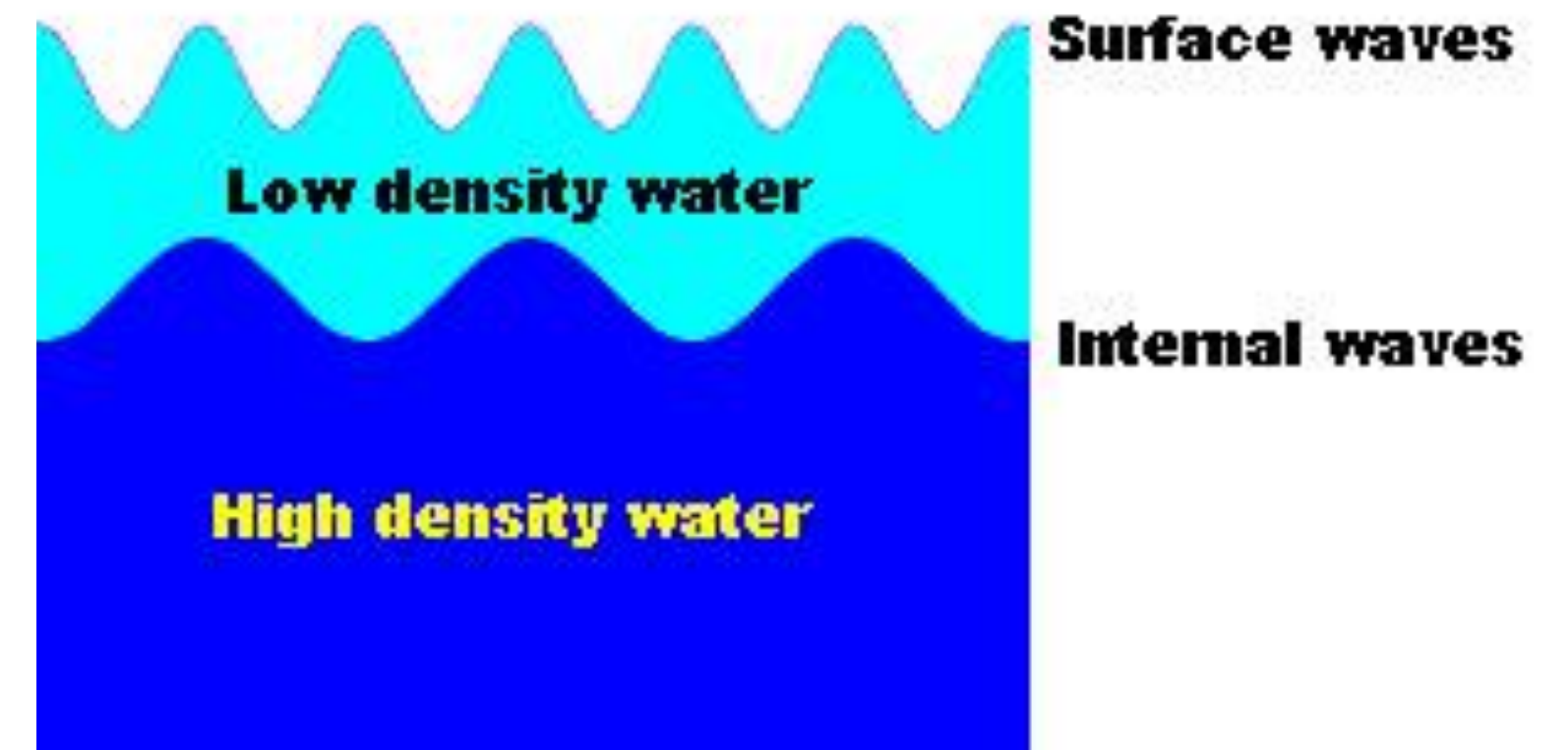
5 Internal waves

<https://www.youtube.com/watch?v=oljinID2yho>

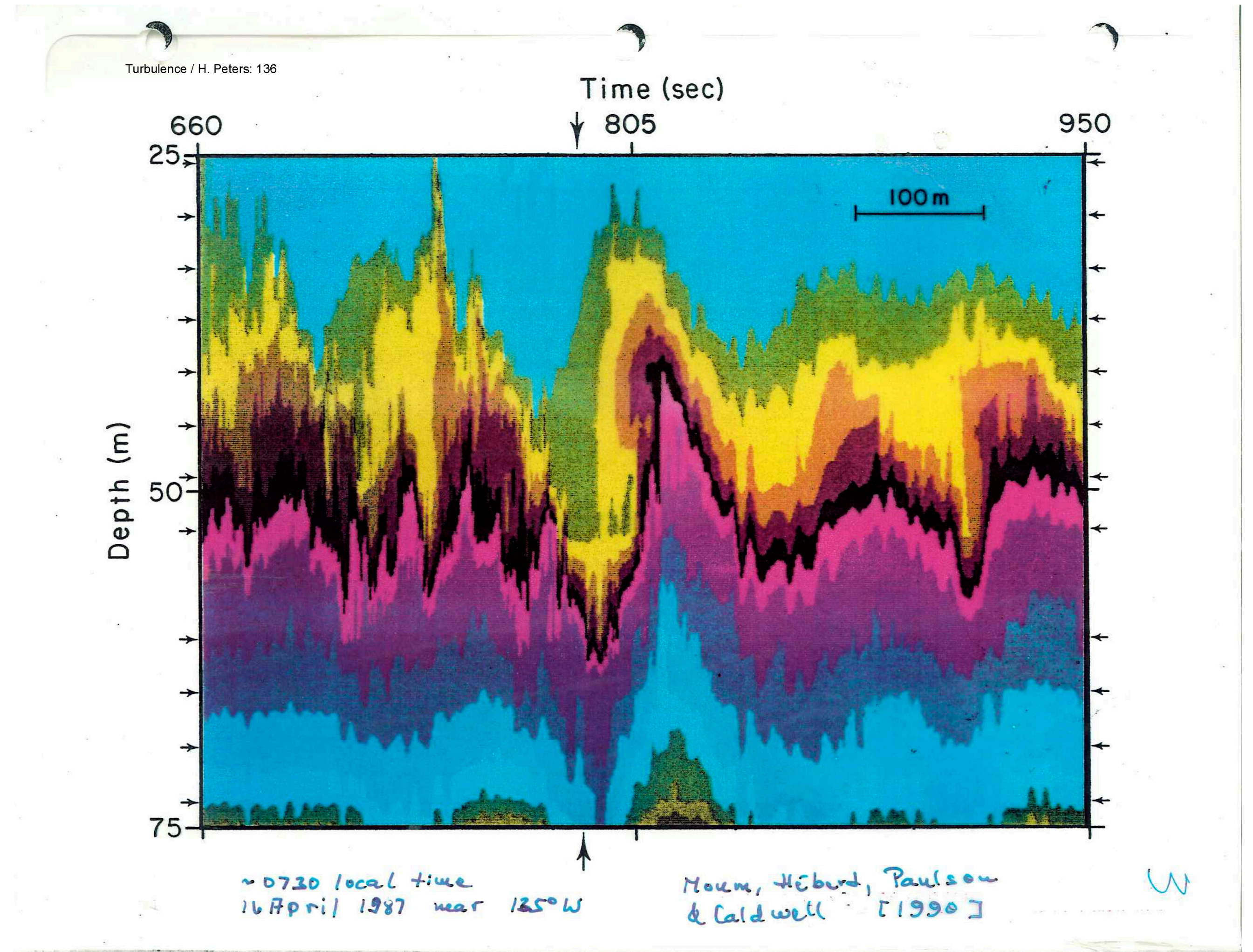
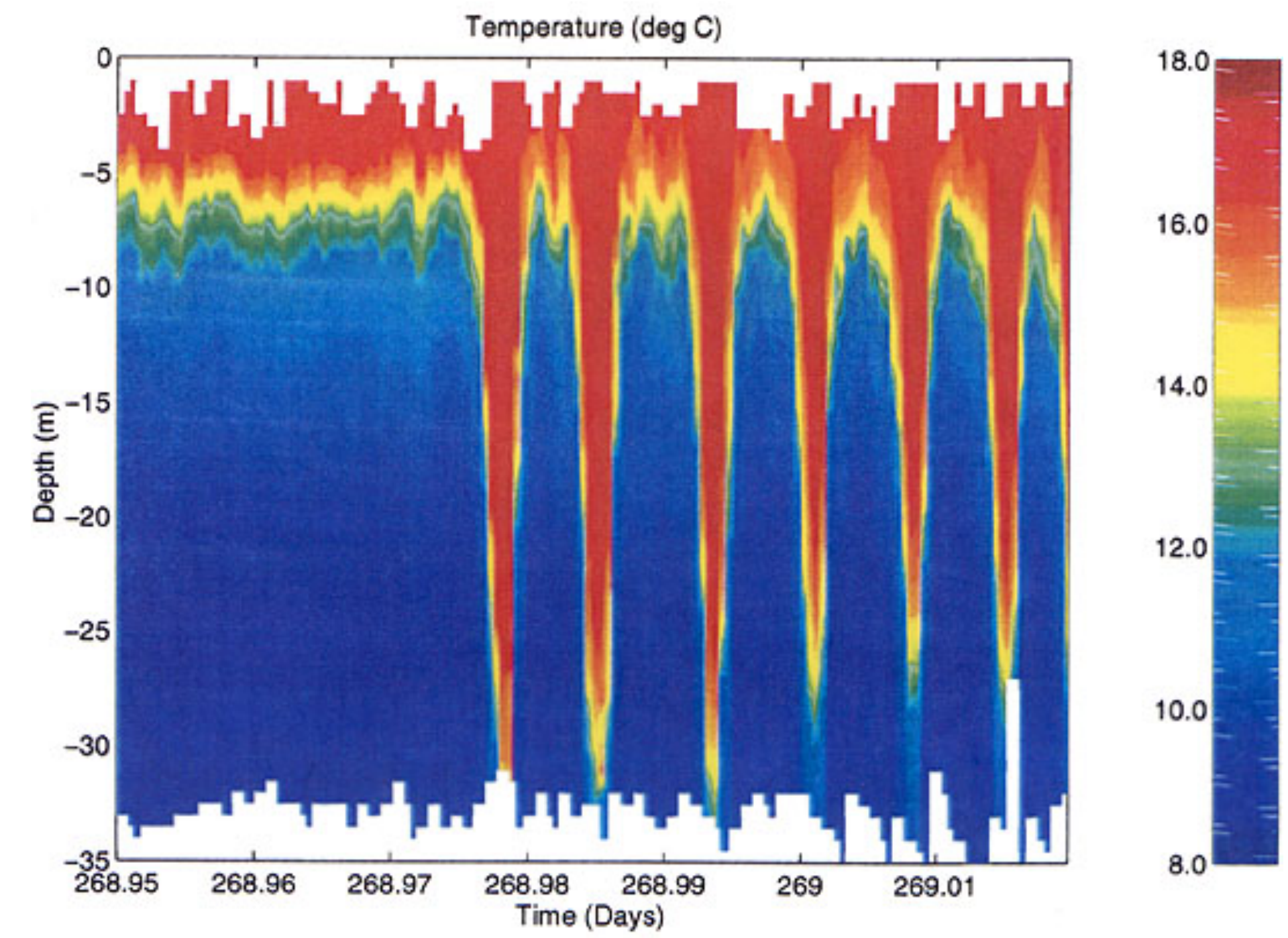


5 Internal waves

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5 Internal waves



5 Internal waves

Dead waters demo



<https://www.youtube.com/watch?v=bzcgAshAg2o>

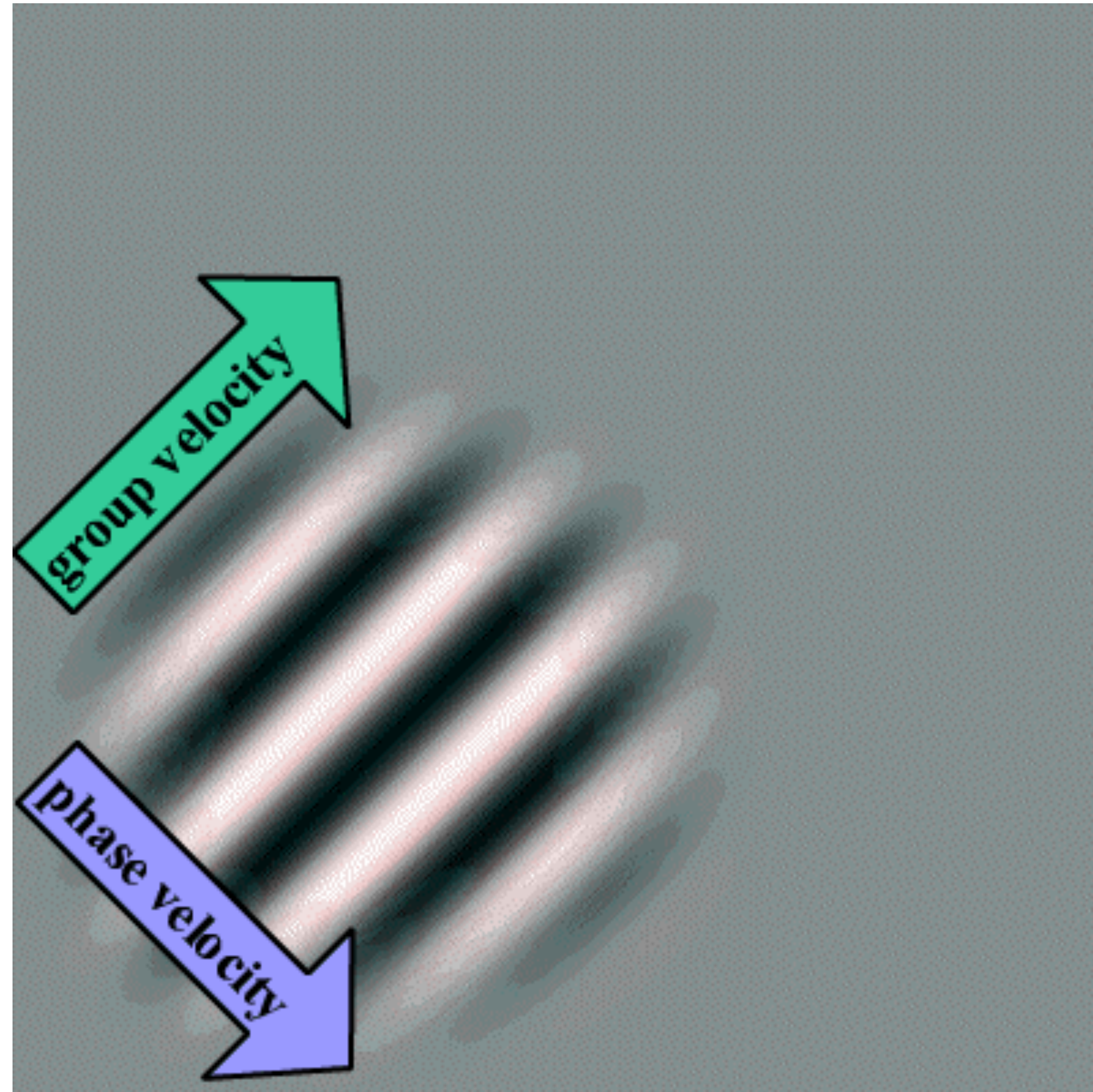
5 Internal waves

Dead waters demo



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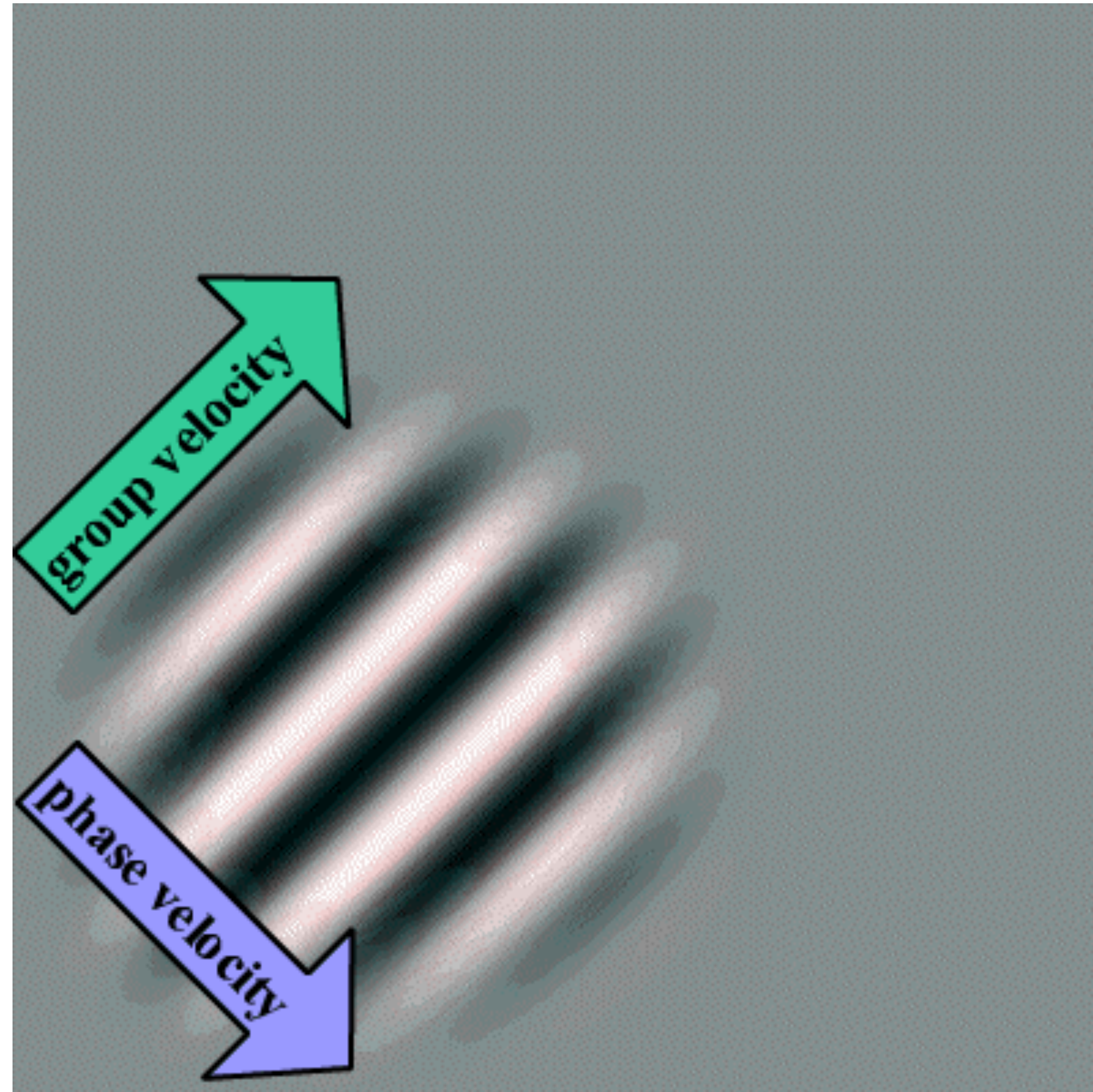
5 Internal waves



The directions of the group velocity and phase velocity of internal waves are orthogonal!



5 Internal waves

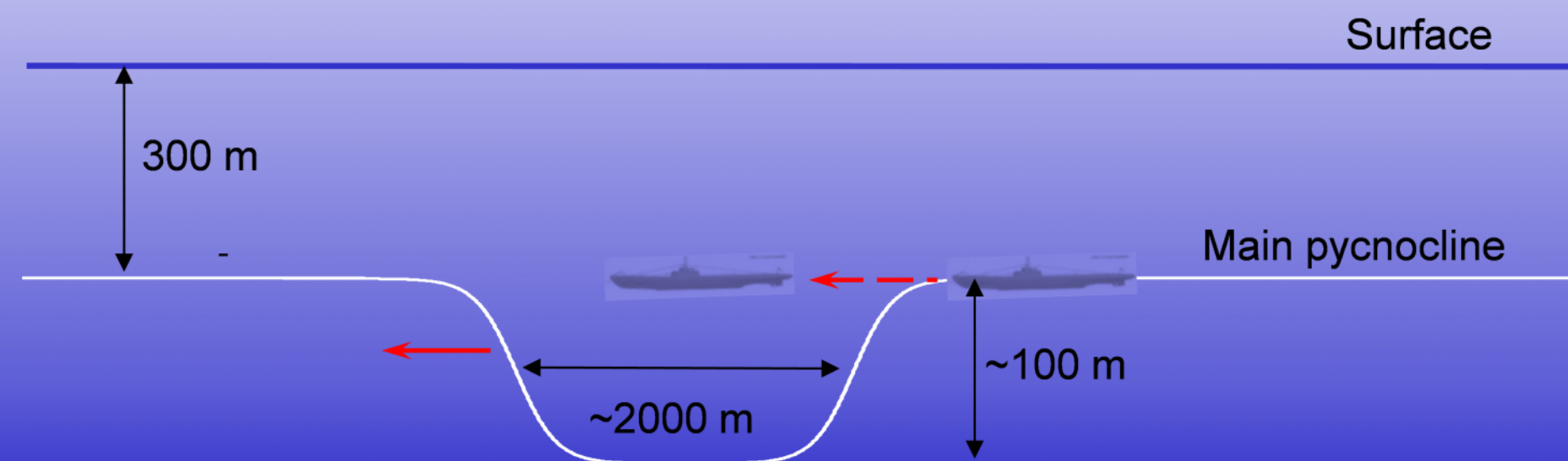


The directions of the group velocity and phase velocity of internal waves are orthogonal!



Internal waves speculations

Stepanyants, Y. (2021) [arXiv](https://arxiv.org/abs/2012.08811): American nuclear submarines, Thresher and Scorpion, perished in the 1960s due to large-amplitude solitary internal waves? Also the diesel Indonesian submarine Nanggala-402...? <https://researchfeatures.com/can-internal-waves-sink-a-submarine/>



An interesting historical possibility is that the effect caused Cleopatra's ships difficulties and loss at the [Battle of Actium](https://en.wikipedia.org/wiki/Battle_of_Actium) in 31 BC in which legend attributes the loss to "suckerfish" attaching to the hulls. https://en.wikipedia.org/wiki/Dead_water



Notes

4 Buoyancy oscillations

Miniquiz

derive equation for buoyancy oscillations

Notes:

5 Internal waves

Notes

6 Shallow water waves in the presence of rotation

6.1 Coastal Kelvin waves



Notes

6 Shallow water waves in the presence of rotation

6.1 Coastal Kelvin waves



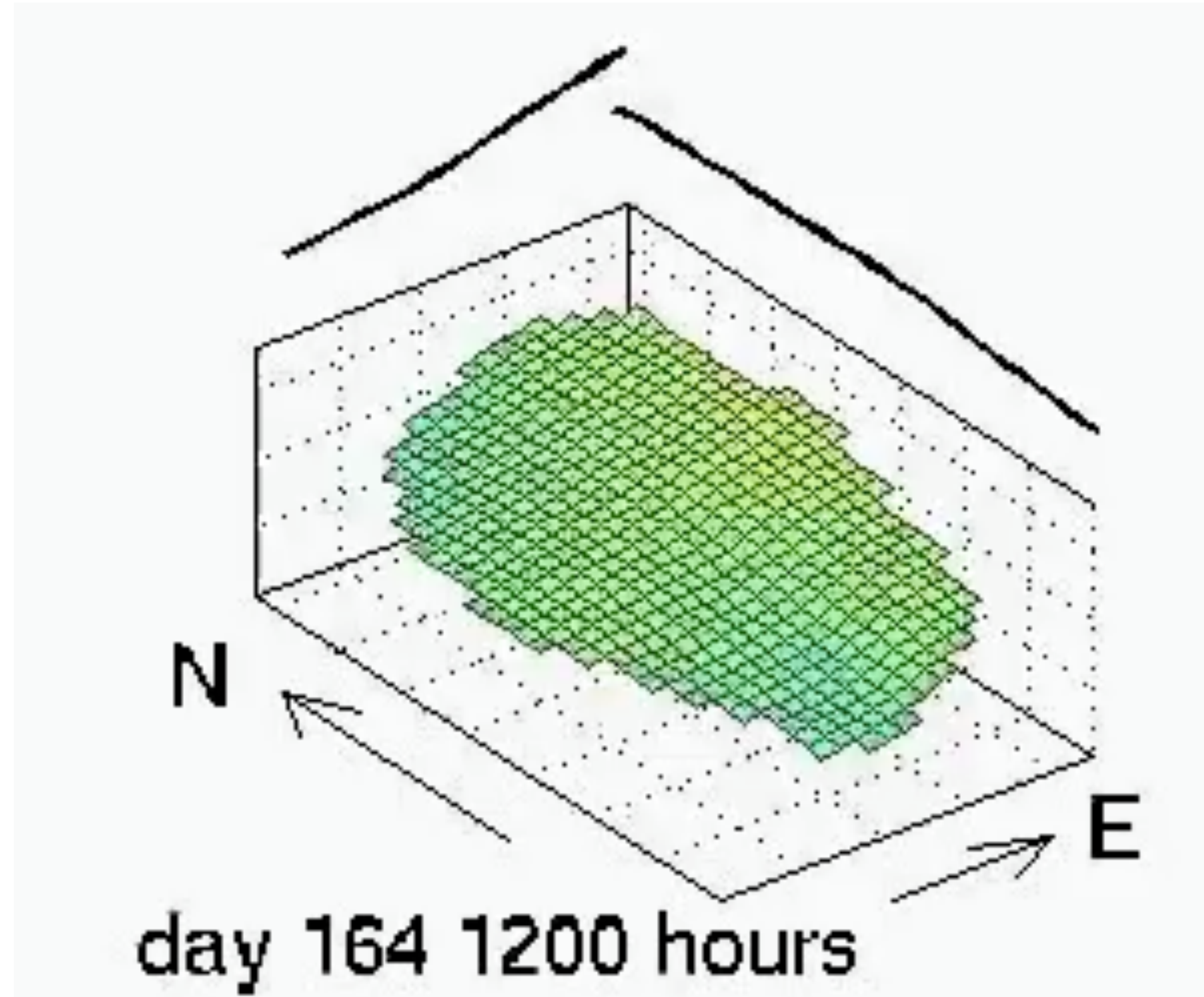
Notes

6 Shallow water waves in the presence of rotation

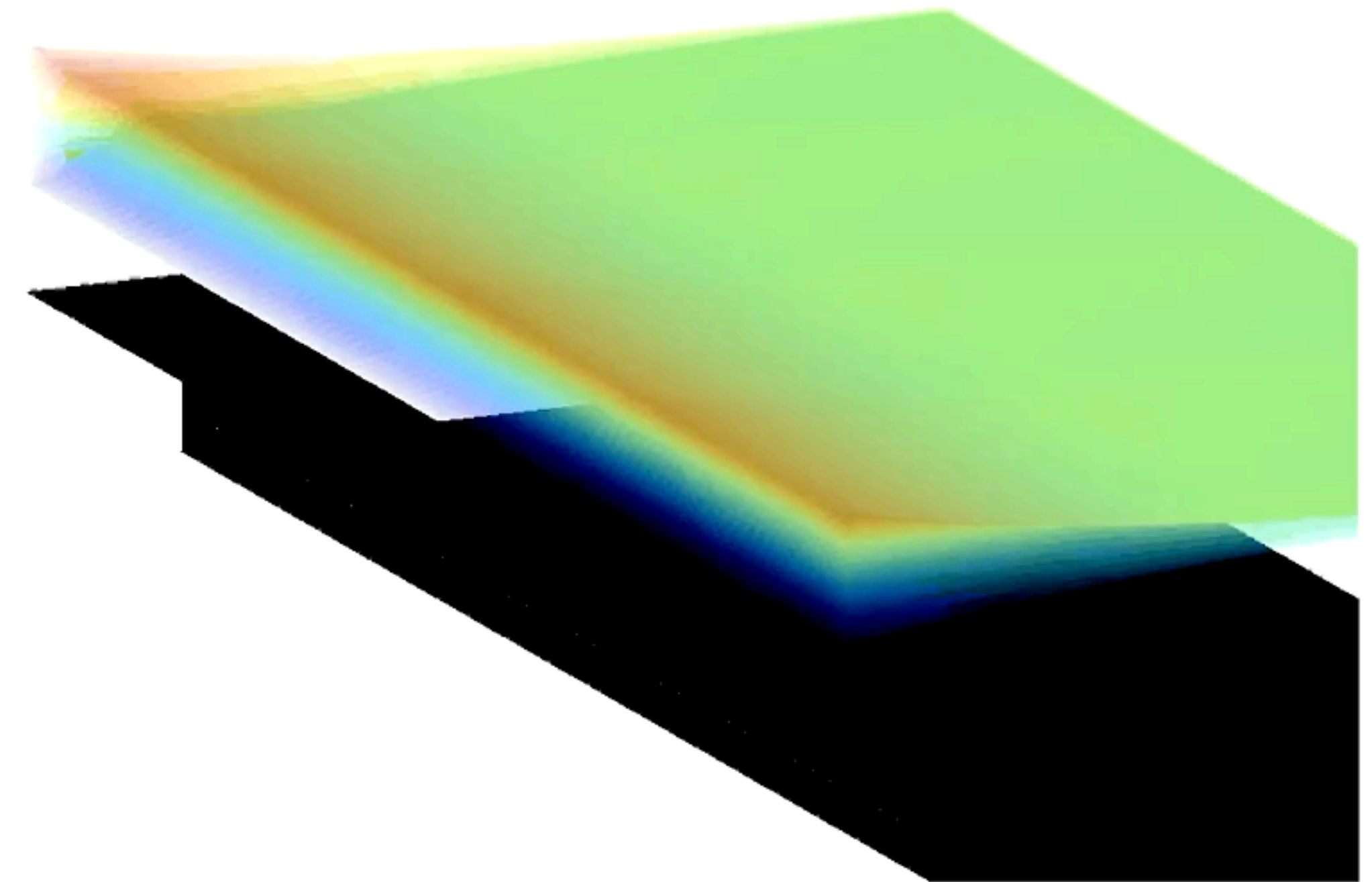
6.1 Coastal Kelvin waves



Coastal Kelvin waves: Lake seiches and along-coast propagation

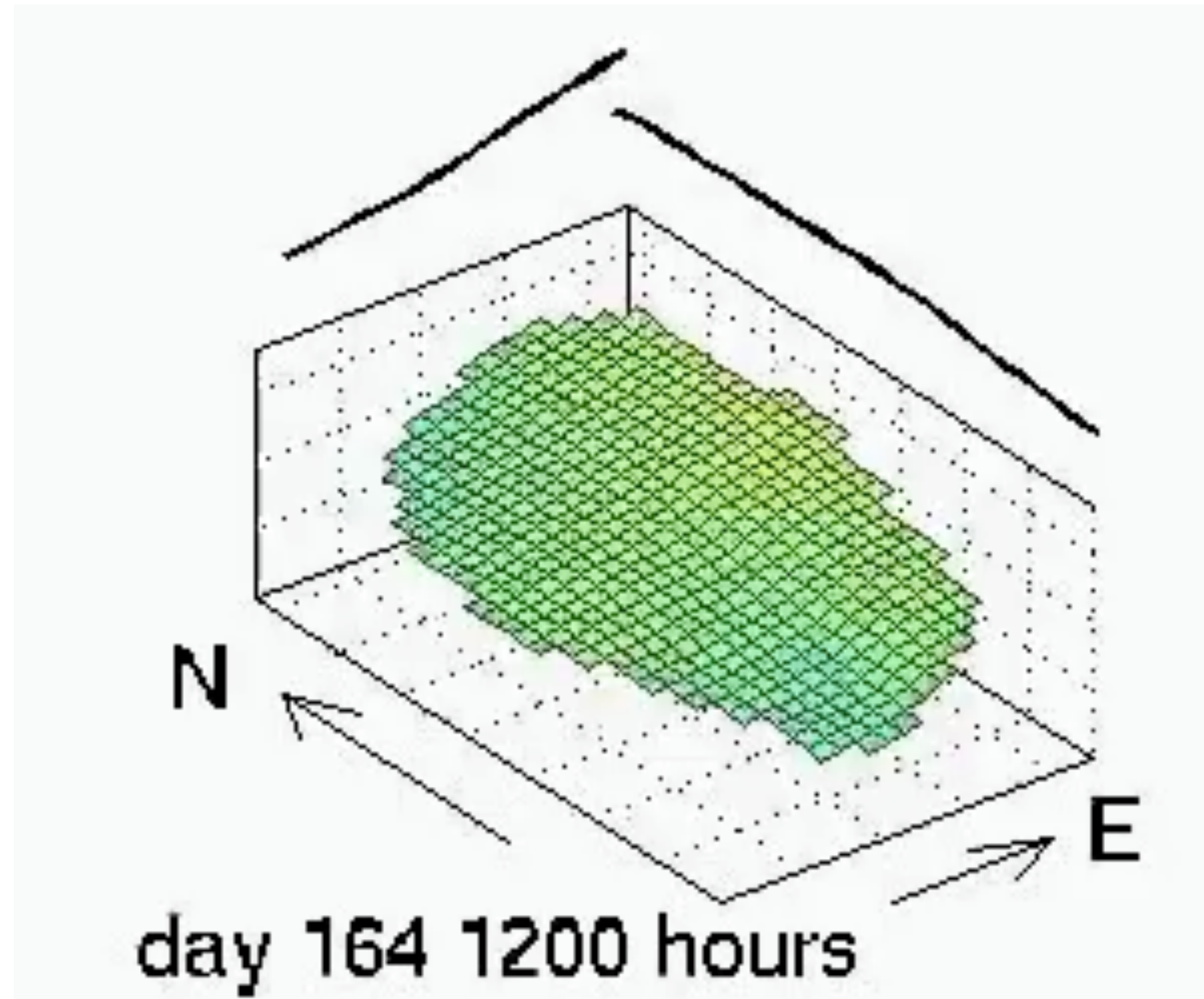


Onda de Kelvin costeira
roberto fioravanti 2010

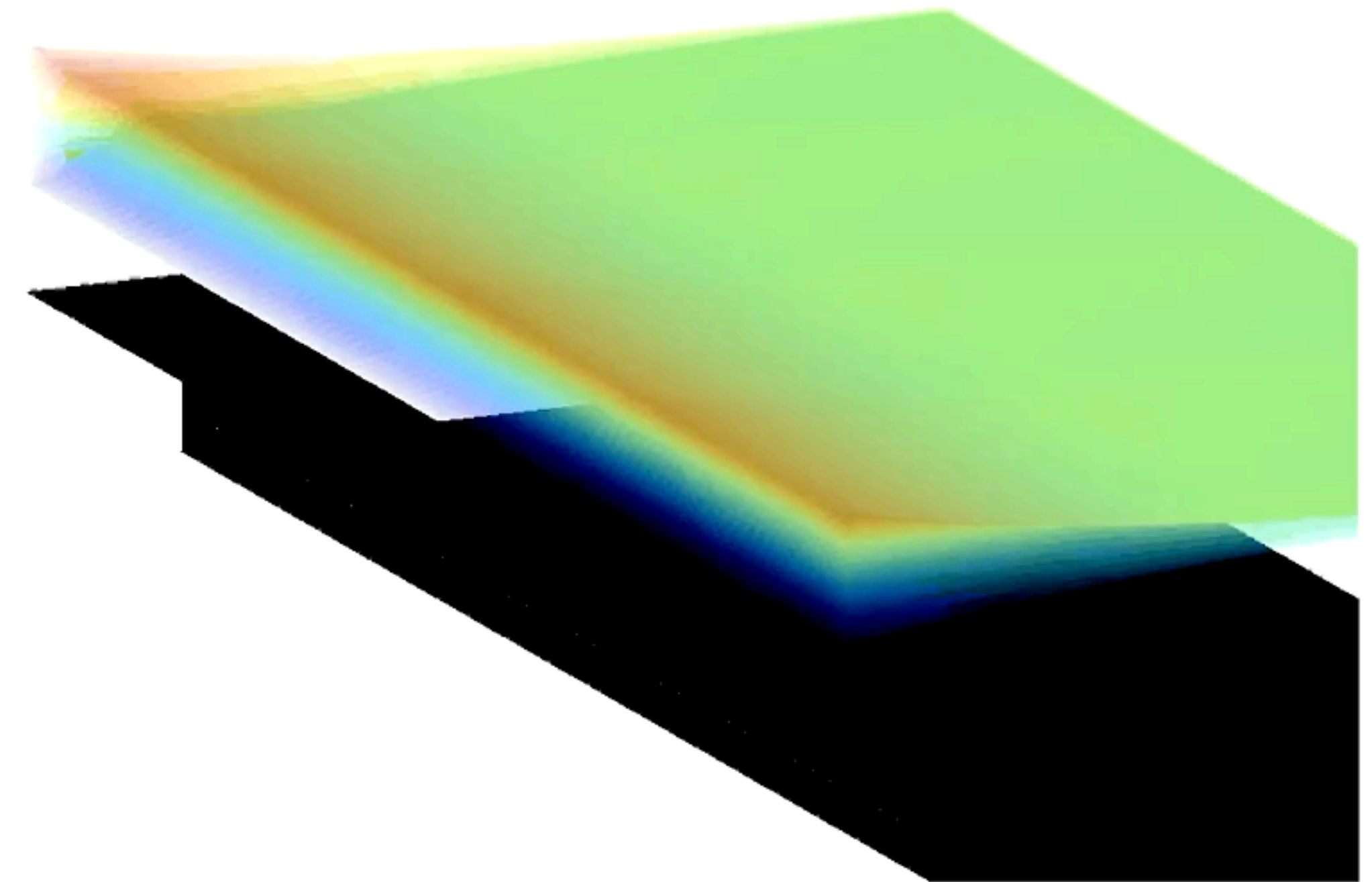


Produced with VideoMach
www.videomach.com

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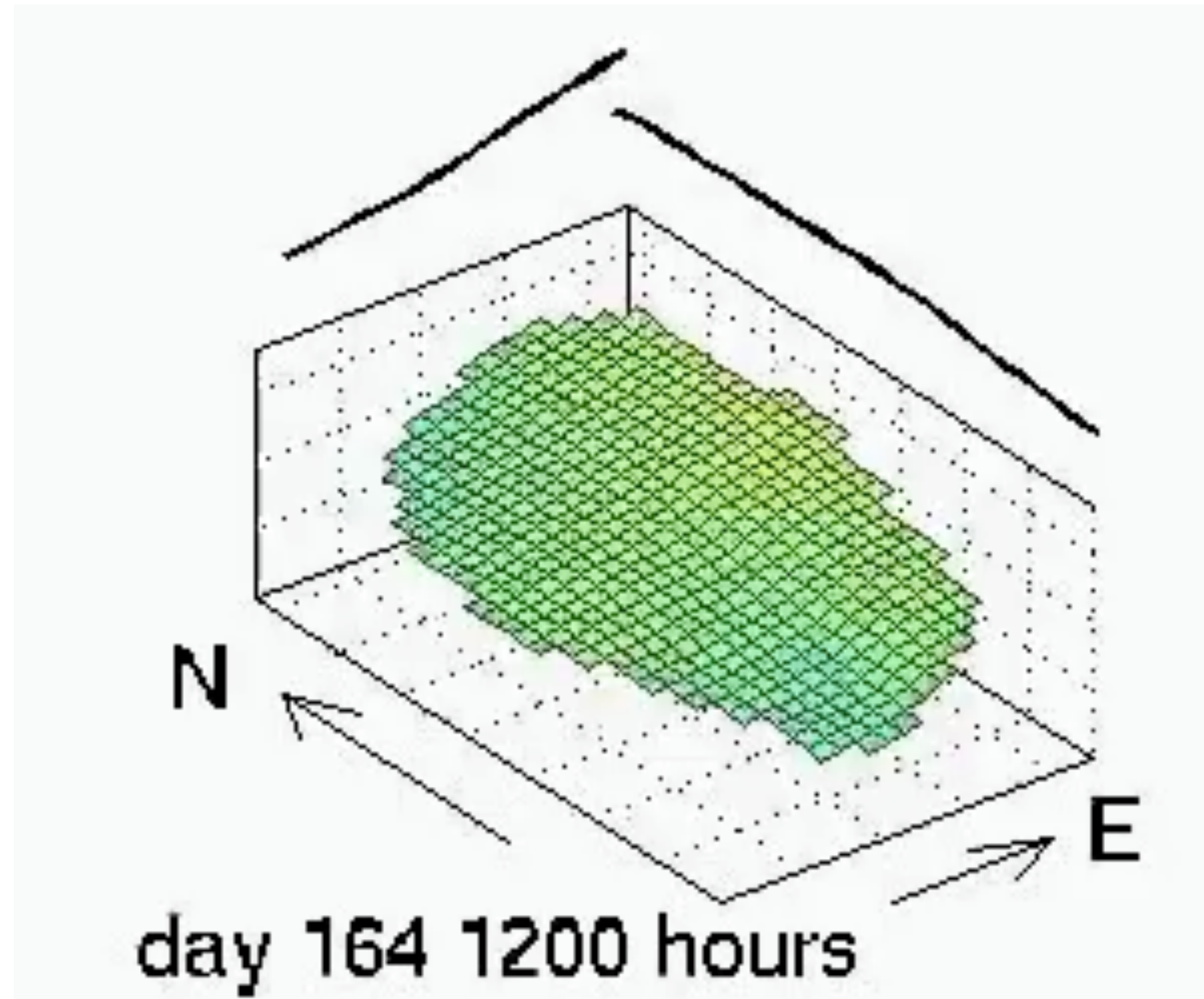


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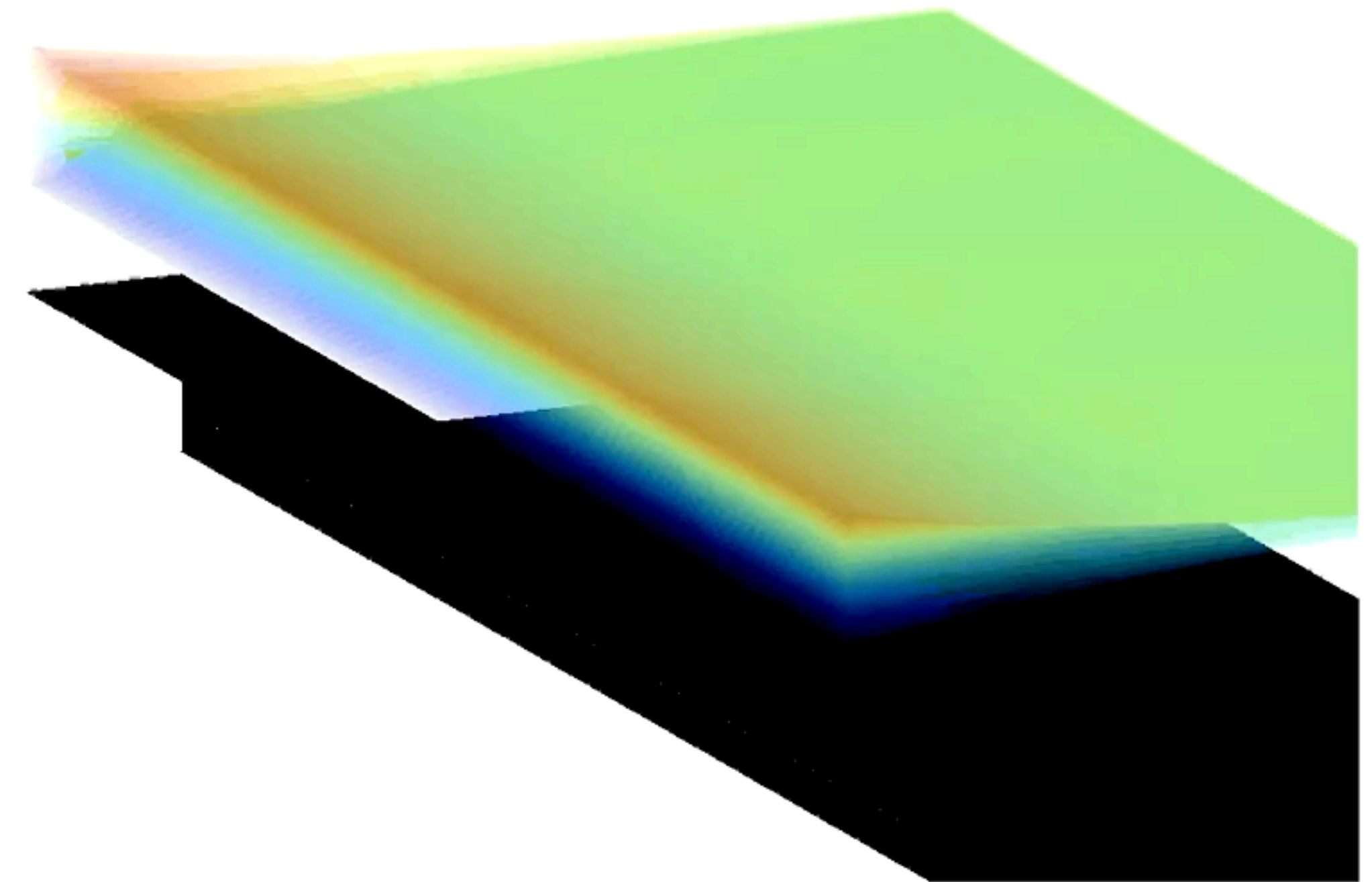


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Coastal Kelvin waves: Lake seiches and along-coast propagation

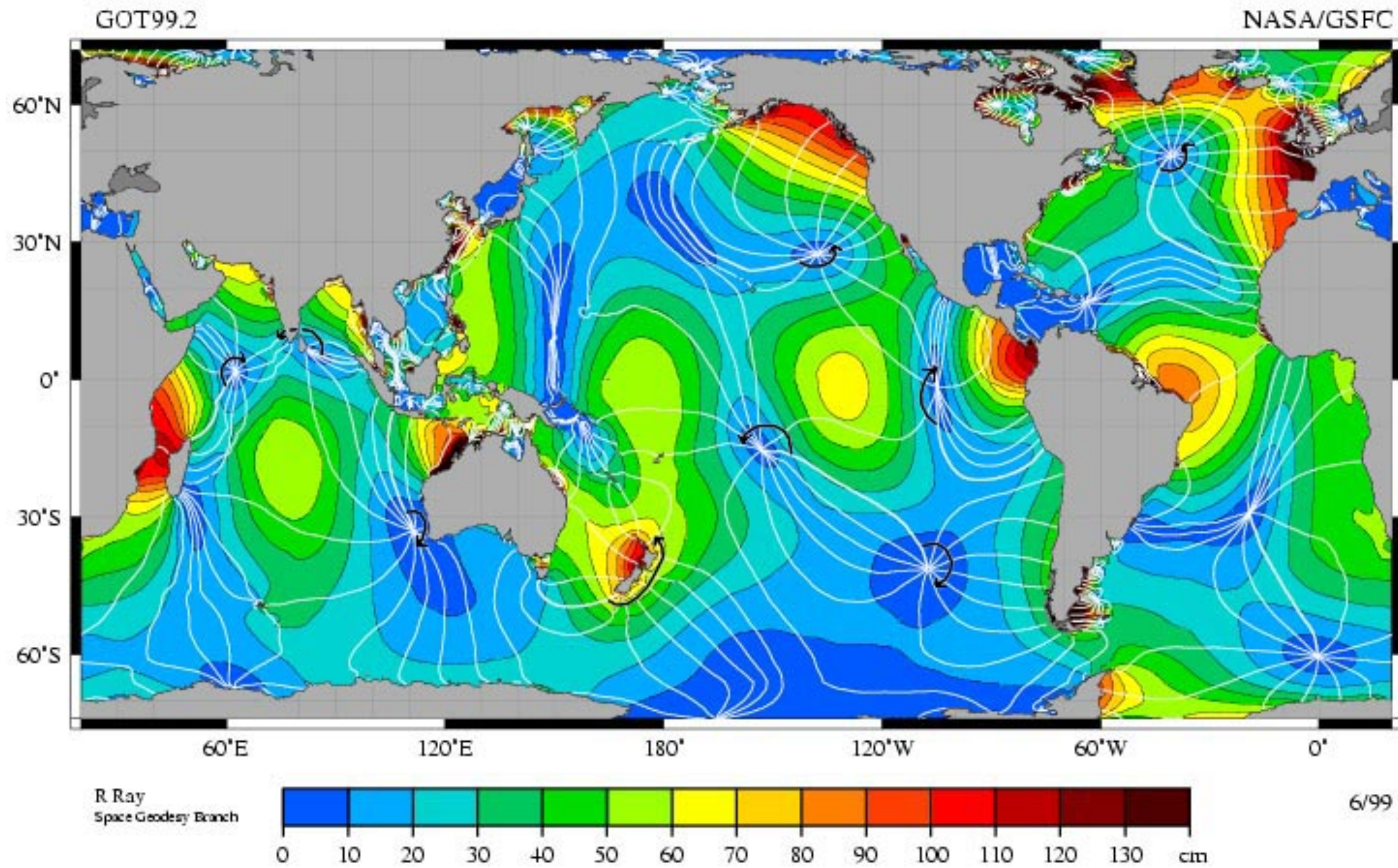


Onda de Kelvin costeira
roberto fioravanti 2010



Produced with VideoMach
www.videomach.com

Coastal Kelvin waves and tidal Amphidromic points



Notes

6 Shallow water waves in the presence of rotation

6.1 Coastal Kelvin waves

Notes

6 Shallow water waves in the presence of rotation

6.2 Poincare waves

The End