CS152: Programming Languages Lecture 17 — Existential Types; Type-and-Effect Systems Dan Grossman Spring 2011	Back to our goal Understand this interface and its nice properties: type 'a mylist; val mt_list : 'a mylist val cons : 'a -> 'a mylist -> 'a mylist val decons : 'a mylist -> (('a * 'a mylist) option) val length : 'a mylist -> int val map : ('a -> 'b) -> 'a mylist -> 'b mylist So far, we can do it <i>if we expose the definition of</i> mylist mt_list : $\forall \alpha.\mu\beta.unit + (\alpha * \beta)$ cons: $\forall \alpha.\alpha \rightarrow (\mu\beta.unit + (\alpha * \beta)) \rightarrow (\mu\beta.unit + (\alpha * \beta))$
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 Abstract Types Define an interface such that well-typed list-clients cannot break the list-library abstraction. Hide the concrete definition of type mylist Why? So clients cannot "forge" lists — always created by library So clients cannot rely on the concrete implementation, which lets us change the library in ways that we know will not break clients To simplify the discussion very slightly, consider just myintlist mylist is a type constructor, a function that given a type gives a type 	The Type-Application Approach We can hide myintlist via type abstraction (like we hid file-handles): $(\Lambda \alpha. \lambda x:\tau_1. list_client) [\tau_2] list_library$ where: τ_1 is { mt : α , cons : int $\rightarrow \alpha \rightarrow \alpha$, decons : $\alpha \rightarrow$ unit + (int * α), } τ_2 is $\mu\beta$.unit + (int * β) $list_client$ projects from record x to get list functions $list_library$ is the record of list functions
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 Evaluating ADT via Type Application (Λα. λx:τ₁. list_client) [τ₂] list_library Plus: Effective Straightforward use of System F Minus: The library does not say myintlist should be abstract It relies on clients to abstract it Can be "fixed" with a "structure inversion" (passing client to the library), but cure arguably worse than disease Different list-libraries have different types, so can't choose one at run-time or put them in a data structure: if n>10 then hashset_lib else listset_lib Wish: values produced by different libraries must have different types, but libraries can have the same type 	<pre>The OO Approach Use recursive types and records: mt_list : μβ. { cons : int → β, decons : unit → (unit + (int * β)), } mt_list is an object — a record of functions plus private data The cons field holds a function that returns a new record of functions Implementation uses recursion and "hidden fields" in an essential way • In ML, free variables are the "hidden fields" • In OO, private fields or abstract interfaces "hide fields" (See Caml code for a slightly different example)</pre>

Evaluating the Closure/OO Approach	The Existential Approach
 Plus: It works in popular languages (no explicit type variables) Different list-libraries have the same type Minus: Changed the interface (no big deal?) Fails on "strong" binary ((n > 1)-ary) operations Have to write append in terms of cons and decons Can be <i>impossible</i> (silly example: see type t2 in ML file) 	 Achieved our goal two different ways, but each had some drawbacks There is a direct way to model ADTs that captures their essence quite nicely: types of the form ∃α.τ Mext slide has a formalization, but we'll mostly focus on The intuition How to use the idea to <i>encode</i> closures (e.g., for callbacks) Why don't many real PLs have existential types? Because other approaches kinda work? Because modules work well even if "second-class"? Because have only been well-understood since the mid-1980s and "tech transfer" takes forever and a day?
Existential Types $e ::= \dots pack \tau, e as \exists \alpha.\tau unpack e as \alpha, x in e \\v ::= \dots pack \tau, v as \exists \alpha.\tau \\\tau ::= \dots \exists \alpha.\tau \\ \underbrace{e \to e'}{pack \tau_1, e as \exists \alpha.\tau_2 \to pack \tau_1, e' as \exists \alpha.\tau_2} \\ \underbrace{e \to e'}{unpack e as \alpha, x in e_2 \to unpack e' as \alpha, x in e_2} \\ unpack (pack \tau_1, v as \exists \alpha.\tau_2) as \alpha, x in e_2 \to e_2[\tau_1/\alpha][v/x] \\ \underbrace{\Delta; \Gamma \vdash e : \tau'[\tau/\alpha]}{\Delta; \Gamma \vdash pack \tau, e as \exists \alpha.\tau' : \exists \alpha.\tau'} \\ \underbrace{\Delta; \Gamma \vdash e_1 : \exists \alpha.\tau' \Delta, \alpha; \Gamma, x : \tau' \vdash e_2 : \tau \Delta \vdash \tau \alpha \notin \Delta \\ \Delta; \Gamma \vdash unpack e_1 as \alpha, x in e_2 : \tau \end{aligned}$	List library with \exists The list library is an existential package: $pack (\mu \alpha.unit + (int * \alpha)), list Jibrary as$ $\exists \beta. \{ empty : \beta, \\ cons : int \rightarrow \beta \rightarrow \beta, \\ decons : \beta \rightarrow unit + (int * \beta), \\ \dots \}Another library would "pack" a different type and implementation, but have the same overall typeBinary operations work fine, e.g., append : \beta \rightarrow \beta \rightarrow \betaLibraries are first-class, but a use of a library must be in a scope that "remembers which \beta" describes data from that library• (If use two libraries in same scope, can't pass the result of one's cons to the other's decons because the two libraries will use different type variables)$
<pre>Closures and Existentials There's a deep connection between existential types and how closures are used/compiled</pre>	<pre>Closures and Existentials C: typedef struct {void* env; void (*f)(void*,int);} * cb_t; Interface: void onKeyEvent(cb_t); Interface: void onKeyEvent(cb_t); Interface: void onKeyEvent(cb_t); Ist_t callBacks = NULL; void onKeyEvent(cb_t cb){callBacks=cons(cb,callBacks); void keyPress(int i) { for(list_t lst=callBacks; lst; lst=lst->tl) lst->hd->f(lst->hd->env, i); } Standard problems using subtyping (t*≤void*) instead of <i>a</i>: Interface: voide an f that downcasts argument back to t* Distender lets library pass any void* to f</pre>



Key facts

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Soundness: If $\cdot \vdash e:\tau;\epsilon$ and e raises uncaught exception s, then $s \in \epsilon$

 Corollary to Preservation and Progress (once you define the operational semantics for exceptions)

All effect systems work this way:

- Values effectless
- Functions have *latent effects*
- Conservative due to if and try/handle

Only a couple rules special to this effect system

 \blacktriangleright Also, not always sets and \cup

More general rules

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Every effect system also substantially more expressive via appropriate subsumption:

- Typing rule for subeffecting (also useful for Preservation)
- Subtyping of functiont types is covariant in latent effects

$$\frac{\Gamma \vdash \tau : e; \epsilon \quad \epsilon \subseteq \epsilon'}{\Gamma \vdash \tau : e; \epsilon'} \qquad \frac{\tau_3 \le \tau_1 \quad \tau_2 \le \tau_4 \quad \epsilon \subseteq \epsilon'}{\tau_1 \stackrel{\epsilon}{\to} \tau_2 \le \tau_3 \stackrel{\epsilon'}{\to} \tau_4}$$

Not shown: Also want effect polymorphism (type variables ranging over effects) for higher-order functions like map

Other examples

- Definitely terminates (true) or possibly diverges (false)
 - ► Give **fix** *e* effect *false*
 - ► Give values effect *true*
 - ► Treat ∪ as and
 - ▶ No change to rules for functions, pairs, conditionals, etc.
- What type casts might occur (*)
- Are the right variables used in transactions (*)
- Does code obey a locking protocol (*)
- Does code only access memory regions that haven't been deallocated (*)
- ► ...

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Really a general way to lift static analysis to higher-order functions

(*) The core technique in a research paper Dan has written, though the idea of using effect systems for this sort of thing is not his

 Key is recognizing "from a mile away" when an effect system is the right tool

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