

CS152, Spring 2011, Reference Sheet for Lecture 3

$$\begin{aligned}
 s &::= \text{skip} \mid x := e \mid s; s \mid \text{if } e \ s \ s \mid \text{while } e \ s \\
 e &::= c \mid x \mid e + e \mid e * e \\
 (c &\in \{\dots, -2, -1, 0, 1, 2, \dots\}) \\
 (x &\in \{x_1, x_2, \dots, y_1, y_2, \dots, z_1, z_2, \dots, \dots\})
 \end{aligned}$$

- Semantics for expressions

1. Informal idea; the need for *heaps*
2. Definition of heaps
3. The evaluation *judgment* (a relation form)
4. The evaluation *inference rules* (the relation definition)
5. Using inference rules
 - *Derivation trees* as interpreters
 - Or as *proofs* about expressions
6. *Metatheory*: Proofs about the semantics

- Then semantics for statements

– ...

$$H(x) = \begin{cases} c & \text{if } H = H', x \mapsto c \\ H'(x) & \text{if } H = H', y \mapsto c' \\ 0 & \text{if } H = . \end{cases}$$

$$\boxed{H ; e \Downarrow c}$$

$$\begin{array}{lll}
 \text{CONST} & \text{VAR} & \text{ADD} \\
 \frac{}{H ; c \Downarrow c} & \frac{}{H ; x \Downarrow H(x)} & \frac{H ; e_1 \Downarrow c_1 \quad H ; e_2 \Downarrow c_2}{H ; e_1 + e_2 \Downarrow c_1 + c_2}
 \end{array}
 \qquad
 \begin{array}{c}
 \text{MULT} \\
 \frac{H ; e_1 \Downarrow c_1 \quad H ; e_2 \Downarrow c_2}{H ; e_1 * e_2 \Downarrow c_1 * c_2}
 \end{array}$$

$$\boxed{H_1 ; s_1 \rightarrow H_2 ; s_2}$$

$$\begin{array}{ccc}
 \text{ASSIGN} & \text{SEQ1} & \text{SEQ2} \\
 \frac{H ; e \Downarrow c}{H ; x := e \rightarrow H, x \mapsto c ; \text{skip}} & \frac{}{H ; \text{skip}; s \rightarrow H ; s} & \frac{H ; s_1 \rightarrow H' ; s'_1}{H ; s_1; s_2 \rightarrow H' ; s'_1; s_2}
 \end{array}
 \qquad
 \begin{array}{c}
 \text{IF1} \quad \text{IF2} \quad \text{WHILE} \\
 \frac{H ; e \Downarrow c \quad c > 0}{H ; \text{if } e \ s_1 \ s_2 \rightarrow H ; s_1} \quad \frac{H ; e \Downarrow c \quad c \leq 0}{H ; \text{if } e \ s_1 \ s_2 \rightarrow H ; s_2} \quad \frac{}{H ; \text{while } e \ s \rightarrow H ; \text{if } e (s; \text{while } e \ s) \ \text{skip}}
 \end{array}$$