Harvard School of Engineering and Applied Sciences — CS 152: Programming Languages

More types Section and Practice Problems

Mar 6-9, 2018

1 Products and Sums

For these questions, use the lambda calculus with products and sums (Lecture 13§1.1).

- (a) Write a program that constructs two values of type $int + (int \rightarrow int)$, one using left injection, and one using right injection.
- (b) Write a function that takes a value of type $int + (int \rightarrow int)$ and if the value is an integer, it adds 7 to it, and if the value is a function it applies the function to 42.
- (c) Give a typing derivation for the following program.

$$\lambda p$$
: (unit \rightarrow int) \times (int \rightarrow int). λx : unit + int. case x of #1 $p \mid \#2$ p

(d) Write a program that uses the term in part (c) above to produce the value 42.

2 Recursion

- (a) Use the μx . e expression to write a function that takes a natural number n and returns the sum of all even natural numbers less than or equal to n. (You can assume you have appropriate integer comparison operators, and also a modulus operator.)
- (b) Try executing your program by applying it to the number 5.
- (c) Give a typing derivation for the following program. What happens if you execute the program?

$$\mu p : (\text{int} \rightarrow \text{int}) \times (\text{int} \rightarrow \text{int}). (\lambda n : \text{int}. n + 1, \#1 p)$$

3 References

(a) Give a typing derivation for the following program.

let
$$a$$
: int ref = ref 4 in let b : (int \rightarrow int) ref = ref λx : int. $x + 38$ in ! b ! a

(b) Execute the program above for 4 small steps, to get configuration $\langle e, \sigma \rangle$. What is an appropriate Σ such that \emptyset , $\Sigma \vdash e : \tau$ and $\Sigma \vdash \sigma$?