

Solution Set 2

1.

x \ yz	00	01	11	10
0	1	1	d	1
1	1	1	d	d

$$F = 1$$

$$= \sum(0, 1, 2, 3, 4, 5, 6, 7)$$

2.

wx \ yz	00	01	11	10
00	1	1	1	1
01		d	1	d
11			d	
10	1		d	1

$$F = \bar{x}\bar{z} + \bar{w}z \quad (\text{sum of products})$$

2. cont'd.

wx \ yz	00	01	11	10
00				
01	0	d		d
11	0	0	d	0
10		0	d	

$$\bar{F} = x\bar{z} + wz$$

$$\therefore F = \overline{x\bar{z} + wz} = \overline{x\bar{z}} \overline{wz} = (\bar{x} + z)(\bar{w} + \bar{z})$$

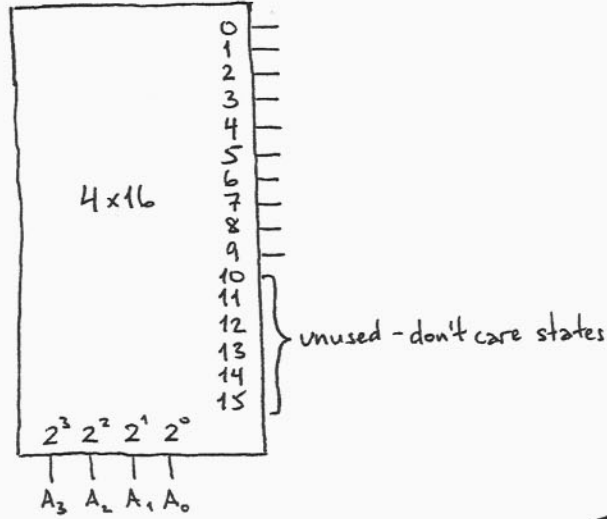
(product of sums)

3.

A \ CD	00	01	11	10
0			1	1
1	1		d	d

$$F = A\bar{D} + C$$

4. BCD is identical to binary except for the binary values 1010 through 1111, which are don't care states in BCD, so we can use a 4x16 decoder.



5.

		yz			
x		00	01	11	10
0	1				
1		1	1		

$$F_1 = \sum(0, 5, 7)$$

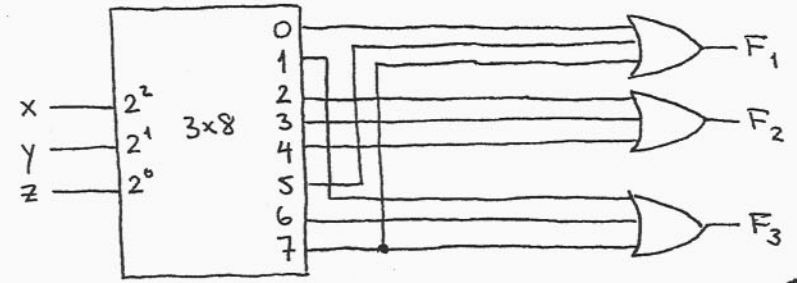
		yz			
x		00	01	11	10
0				1	1
1	1				

$$F_2 = \sum(2, 3, 4)$$

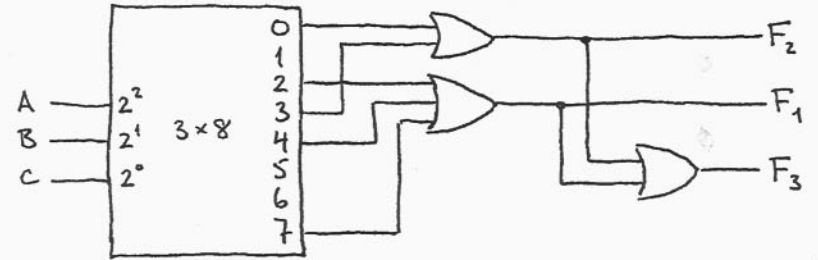
		yz			
x		00	01	11	10
0			1		
1				1	1

$$F_3 = \sum(1, 6, 7)$$

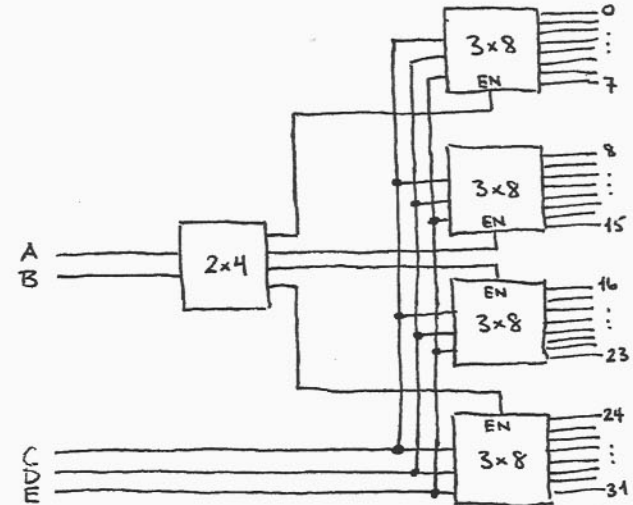
5. cont'd.



6.



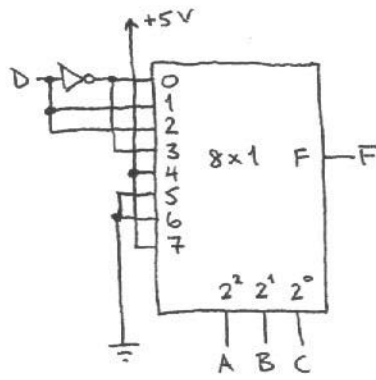
7.



8.

A	B	C	D	F
0	0	0	0	1
0	0	0	1	0
0	0	1	0	0
0	0	1	1	1
0	1	0	0	0
0	1	0	1	1
0	1	1	0	1
0	1	1	1	0
1	0	0	0	1
1	0	0	1	1
1	0	1	0	0
1	0	1	1	0
1	1	0	0	0
1	1	0	1	0
1	1	1	0	1
1	1	1	1	1

$F = \bar{D}$
 $F = D$
 $F = D$
 $F = D$
 $F = \bar{D}$
 $F = 1$
 $F = 1$
 $F = 0$
 $F = 0$
 $F = 0$
 $F = 1$

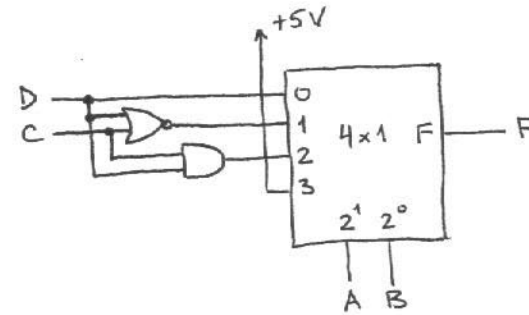


→ type 1 implementation.

10.

A	B	C	D	F
0	0	0	0	0
0	0	0	1	1
0	0	1	0	0
0	0	1	1	1
0	1	0	0	1
0	1	0	1	0
0	1	1	0	0
0	1	1	1	0
1	0	0	0	0
1	0	0	1	0
1	0	1	0	0
1	0	1	1	1
1	1	0	0	1
1	1	0	1	1
1	1	1	0	1
1	1	1	1	1

$F = D$
 $F = C + D$
 $F = CD$
 $F = 1$



→ type 2 implementation.

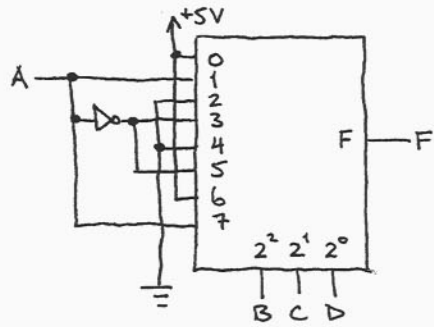
9.

A	B	C	D	F
0	0	0	0	0
0	0	0	1	1
0	0	1	0	0
0	0	1	1	0
0	1	0	0	0
0	1	0	1	0
0	1	1	0	1
0	1	1	1	1
1	0	0	0	0
1	0	0	1	1
1	0	1	0	1
1	0	1	1	1
1	1	0	0	1
1	1	0	1	0
1	1	1	0	0
1	1	1	1	0

$F = \Sigma(1, 6, 7, 9, 10, 11, 12)$

8.

\bar{A}	0	1	2	3	4	5	6	7
A	8	9	10	11	12	13	14	15
	1	A	0	\bar{A}	0	\bar{A}	1	A

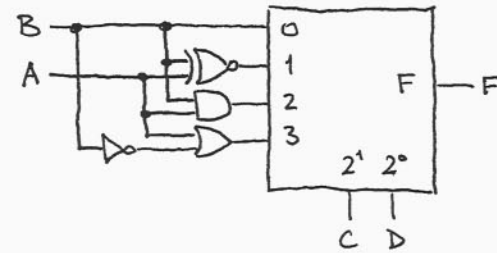


Other solutions exist depending on the choice of select inputs.

10.

$\bar{A}\bar{B}$	0	1	2	3
$\bar{A}B$	4	5	6	7
$A\bar{B}$	8	9	10	11
AB	12	13	14	15

$\bar{A}\bar{B} + AB$ $A + \bar{B}$ — you may know this as $A \rightarrow B$ in logic
 $= A \odot B$



9.

$$F(A, B, C, D) = \sum (1, 6, 7, 9, 10, 11, 12)$$

$$F(D, A, B, C) = \sum (3, 5, 6, 8, 11, 12, 13)$$

The first form is preferable. When using any other order of variables (such as D, A, B, C) they must be explicitly stated.